Toward polarized antiprotons: Machine development for spin-filtering experiments

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The paper describes the commissioning of the experimental equipment and the machine studies required for the first spin-filtering experiment with protons at a beam kinetic energy of 49.3 MeV in COSY. The implementation of a low- β insertion made it possible to achieve beam lifetimes of $\tau_b = 8000$ s in the presence of a dense polarized hydrogen storage-cell target of areal density $d_t = (5.5 \pm 0.2) \times 10^{13}$ atoms/cm². The developed techniques can be directly applied to antiproton machines and allow the determination of the spin-dependent $\bar{p}p$ cross sections via spin filtering.

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I. INTRODUCTION

As long ago as 1968 it was realized that by means of a spin filter using an internal polarized hydrogen target polarized high-energy proton beams could be produced at the 30 GeV intersecting storage ring (ISR) at CERN [1].

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Since more efficient methods of providing polarized beams had already been developed, the idea of using a spin filter was revisited only in 1982 to polarize antiprotons at the low-energy antiproton-cooler ring (LEAR) of CERN [2]. At the 1985 workshop at Bodega Bay, CA, USA, a number of different techniques were discussed for providing stored beams of antiprotons [3]. Of these techniques, spin filtering was considered practical and promising.

Spin filtering and related mechanisms leading to a polarization buildup in a stored beam were discussed in great detail at the Daresbury workshop in 2007 [4], and in a WE-Heraeus seminar in 2008 at Bad Honnef, Germany [5]. In the framework of the FILTEX collaboration, polarization

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buildup in an initially unpolarized beam was observed for the first time using 23 MeV protons stored in the test storage ring (TSR) at Heidelberg, interacting with polarized hydrogen atoms in a storage-cell target [6]. (A detailed description of the experimental effort is given in [7–9], upto-date results are summarized in [10].)

The renewed interest in experiments with polarized antiprotons aims to produce a polarized antiproton beam at the high-energy storage ring (HESR) [11] of the facility for antiproton and ion research (FAIR) [12] in Darmstadt, Germany. In 2003, a Letter of Intent for a variety of spinphysics experiments with polarized antiprotons was proposed by the polarized antiproton experiments (PAX) collaboration [13]. In 2005, the PAX collaboration submitted a technical proposal to the QCD program committee of FAIR, suggesting as an upgrade for HESR a doublepolarized antiproton-proton collider to study, among other subjects, the transversity distribution of the proton [14,15].

Polarizing a stored beam by spin flip in polarized electron-proton (\vec{e}^-p) or polarized positron-antiproton $(\vec{e}^+\bar{p})$ scattering [16] presents an advantage, because in contrast to spin filtering beam particles are not lost. Triggered by the PAX proposal, the theory of spin-flip interactions was radically revised, leading to negligibly small cross sections for proton-electron scattering [17–20]. In a recent experiment performed at the cooler synchrotron and storage ring (COSY) [21], the $e^-\vec{p}$ spin-flip cross sections were indeed shown to be too small to allow the efficient production of polarized antiprotons based on $e^+\bar{p}$ interactions [10,22].

Polarizing antiprotons by spin filtering, using the spindependent part of the nucleon-nucleon interaction, remains as yet the only viable method experimentally confirmed for a stored beam of protons and a polarized hydrogen gas target [6,7]. Theoretical considerations for beams of antiprotons have meanwhile been extended from $\bar{p} \vec{H}$ interactions [23,24] to $\bar{p} \vec{D}$ [25] and $\bar{p}^3 \vec{H}e$ [26].

In order to complement the Heidelberg TSR spinfiltering experiment by a second measurement, and to commission the experimental setup for the proposed $\bar{p}p$ experiment at the antiproton decelerator (AD) of CERN [27], a spin-filtering experiment was performed in 2011 at COSY. The experiment confirmed that only pp scattering contributes to the polarization buildup [28]. At a beam kinetic energy of T = 49.3 MeV, slightly above the COSY injection energy of T = 45 MeV, precise $\vec{p}d$ analyzing power data for the beam polarization measurement are available [29].

The spin-filtering method exploits the spin dependence of the total hadronic cross section [30],

$$\sigma_{\rm tot} = \sigma_0 \pm \sigma_1 \cdot Q, \tag{1}$$

where σ_0 is the spin-independent part, σ_1 the spindependent part, and Q is the nuclear polarization of the target. The positive (negative) signs denote a parallel (antiparallel) orientation of the spins of beam and target protons.

The number of beam protons with spin orientation parallel (antiparallel) to that of the target spins is denoted by N^{\uparrow} (N^{\downarrow}). One can safely neglect the numerically minuscule spin-flip cross section. Then the decrease of the total number of beam particles as a function of time from the initial values $N^{\uparrow}(t=0) = N^{\downarrow}(t=0) = N_{\text{tot}}(t=0)/2$ is described by

$$N_{\text{tot}}(t) = N^{\uparrow}(t) + N^{\downarrow}(t)$$

= $N_{\text{tot}}(0) \cdot \exp\left(-\frac{t}{\tau_b}\right) \cdot \cosh\left(\frac{t}{\tau_1}\right),$ (2)

where

$$\tau_b = (d_t f \sigma_b)^{-1}$$
 and $\tau_1 = (Q d_t f \tilde{\sigma}_1)^{-1}$. (3)

Here d_t is the areal target gas density, f is the revolution frequency determined by the beam momentum and the ring circumference, and $\tilde{\sigma}_1 = \sigma_1(\Theta > \Theta_{acc})$ represents the effective removal cross section. Furthermore, $\sigma_b = \sigma_0 + \sigma_C$ combines σ_0 and single Coulomb scattering σ_C in the target, the latter for scattering angles larger than the acceptance angle Θ_{acc} of the machine. For single Coulomb scattering and small values of Θ_{acc} , the beam lifetime $\tau_b \propto \sigma_C^{-1} \propto$ $\Theta_{acc}^2 \propto \beta^{-1}$ (see Sec. II B). Therefore the betatron function (or β -function) at the target should be small in order to achieve a long beam lifetime.

The polarization buildup in the stored, circulating beam is given by

$$P(t) = \frac{N^{\uparrow}(t) - N^{\downarrow}(t)}{N^{\uparrow}(t) + N^{\downarrow}(t)} = \tanh\left(\frac{t}{\tau_1}\right).$$
(4)

It depends on the spin-dependent removal of particles. The effective removal cross section in (3) depends on the machine acceptance and consequently so does the achievable beam polarization, as illustrated, e.g., in Fig. 15 of [24].

The present paper describes the development effort, including a variety of measurements, necessary to prepare the COSY storage ring and the experimental equipment for the spin-filtering experiments [28,31]. The paper is organized as follows:

Section II presents the essential components of the COSY ring, in particular its lattice and the electron cooler (II A), followed by the requirements for the low- β insertion at the position of the polarized gas target, and its realization (II B).

Section III describes the internal polarized hydrogen storage-cell target (III A), the coil system to produce the magnetic holding field at the storage cell (III B), and the vacuum system around the polarized target (III C).

In Sec. IV the equipment employed for beam diagnosis is described, comprising the beam current transformer, H⁰ monitor, ionization profile monitor, beam-position monitor, movable frame system for acceptance measurements, and beam polarimeter.

Section V describes the betatron tune mapping (Sec. VA) and orbit adjustment (Sec. VB) to provide long beam lifetime for the spin-filtering experiments.

Section VI highlights the commissioning of the low- β insertion, including the determination of the β -function at the target.

Section VII presents the measurements of the beamwidths (VII A) at the location of the internal target, the beam emittance (VII B), and the determination of the machine acceptance and the acceptance angle at the target position (VII C).

In Sec. VIII the efforts are described to optimize the beam lifetime by means of closed orbit correction and tune adjustment. Space-charge effects (VIII A) and vacuum considerations are discussed as well (VIII B).

In Sec. IX it is explained how the beam was set up for the experiments (IX A) and what a typical measurement cycle looked like (IX B). In addition, the measurement of the beam polarization lifetime (IX C) and the efficiency of the rf spin flipper are described (IX D).

Section X summarizes the main results.

II. COSY ACCELERATOR AND STORAGE RING

The synchrotron and storage ring COSY accelerates and stores unpolarized and polarized proton or deuteron beams in the momentum range between 0.3 GeV/c and 3.65 GeV/c. COSY has a racetrack design with two 180° arc sections connected by 40 m long straight sections. It is operated as a cooler storage ring with internal targets, such as the apparatus for studies of nucleon and kaon ejectiles (ANKE), the wide angle shower apparatus (WASA), and the PAX interaction point, or with an extracted beam (see Fig. 1, bottom panel). Beam cooling, i.e., reducing the momentum spread of the beam and shrinking the transverse equilibrium phase space, is realized by electron cooling up to proton-beam momenta of 0.6 GeV/c [32] and by stochastic cooling for proton momenta above 1.5 GeV/c [33].

Polarized proton and deuteron beams are routinely delivered to experiments over the whole momentum range [34]. Polarized beams from the ion source are preaccelerated in the cyclotron JULIC [35], injected and accelerated in COSY without significant loss of polarization. Imperfection and intrinsic depolarization resonances are overcome by well-established procedures [36–38]. When the polarization lifetime is by several orders of magnitude longer than the spin filtering periods required, it becomes feasible to polarize an originally unpolarized beam by filtering, as was confirmed in a dedicated experiment [28], described in Sec. IX.



FIG. 1. Bottom panel: Floor plan of the COSY facility. The 24 dipole magnets are shown in red, the quadrupole magnets in blue except those around the PAX target point (PAX-TP) and the 100 keV electron cooler which are shown in green. The quadrupole magnets of COSY are combined into quadrupole families, each consisting of four magnets with a common current supply. There are eight families for the telescopic straight sections (QT1 to QT8, middle panel) and six for the arcs (QU1 to QU6, top panel). The PAX quadrupoles of the low- β insertion at the PAX-TP are combined into an outer pair (PAX1) and an inner pair (PAX2).

A. COSY lattice and electron cooler

The COSY lattice is designed to provide flexibility with respect to ion-optical settings [39] in order to fulfill the requirements for internal and external experiments. Each of the arcs is composed of three mirror-symmetric unit cells (U) consisting of four dipole magnets (O), two horizontally focusing (F) and two horizontally defocusing quadrupole magnets (D). Each of the six unit cells has a DOFO-OFOD structure (see Fig. 1, top panel). The two inner (and outer) quadrupole magnets of each unit cell are connected to the inner (and outer) pair of the opposite unit cell located in the other arc, thus resulting in six quadrupole families (QU1 to QU6). A symmetric operation of all unit cells leads to a sixfold symmetry of the β -functions [40].

The straight sections are composed of two mirrorsymmetric telescopic (T) arrangements with two quadrupole triplets, each consisting of four quadrupoles, either operated in FDDF or DFFD mode. A 2π phase advance and 1:1 imaging over the complete straight section is thus achieved, decoupling to first order the arcs from the straight sections [39] and providing three possible locations per straight section for internal target experiments with adjustable β -functions in the center of the triplets. Figure 2 (top panel) shows the horizontal (*x*) and vertical (*y*) β -functions, β_x and β_y , and the dispersion *D* for a typical setting of COSY used at injection. The basic parameters of COSY are listed in Table I.

The straight sections can be made free of dispersion by breaking the sixfold symmetry with a specific setting of the six arc quadrupole families (see Fig. 2, bottom panel).



FIG. 2. Top panel: Optical functions (β_x, β_y) and dispersion *D* along COSY for a standard setting $(D \neq 0)$. In each of the arcs symmetric behavior due to the three unit cells in each section can be seen. Bottom panel: β -functions and dispersion for the D = 0 setting through the telescopes. The PAX target is located in the center of the target telescope.

TABLE I.	Main	parameters	of	the	COSY	accelerator	and
storage ring	[21].						

COSY					
Circumference	183.47 m				
Particles	(Un)polarized p and d				
Type of injection	H^- , D^- stripping injection				
Current at source exit	Polarized: 15 μ A				
	Unpolarized: 100-200 µA				
Momentum range	0.3–3.65 GeV/c				
Betatron tune range	3.55–3.7 in both planes				
Phase-space cooling	Electron and stochastic				
Beam position monitors	31 (horizontal and vertical)				
Steerers	23 (horizontal), 21 (vertical)				
Straight sections	Length: 40 m				
-	4×4 quadrupole magnets				
	4 sextupole magnets				
	Beam pipe diameter: 0.15 m				
Arc sections	Length: 52 m				
	3×4 dipole magnets				
	3×4 quadrupole magnets				
	5 sextupole magnets				
	Beam pipe in dipole magnets:				
	height: 0.06 m, width: 0.15 m				

This dispersion-free D = 0 setting is advantageous for the operation of the storage-cell target, and it was therefore chosen during the spin-filtering experiments. A nonzero dispersion causes a displacement of a particle with a relative momentum deviation $\frac{\Delta p}{p}$ from the reference orbit x_{ref} and the deviation from the ideal orbit is given by [41]

$$x(s)_{\text{total}} = x_{\text{ref}}(s) + D(s) \cdot \frac{\Delta p}{p},$$
(5)

where *s* is the position along the reference orbit and s = 0 is located at the beginning of the straight section where the PAX-TP is located.

The COSY electron cooler (see Fig. 1) is used to compensate multiple small-angle Coulomb scattering and energy loss in the target and the residual gas in the machine. It provided stable beam emittance and beam energy during the spin-filtering experiment. It was designed for electron energies up to 100 keV, thus enabling phase-space cooling up to a proton-beam kinetic energy of 183.6 MeV [42]. Its main parameters are listed in Table II. Two short solenoids located in the 8 m long drift region in front of and behind the electron cooler (see Fig. 7 of [43]) and operated with reversed polarity to that in the drift solenoid compensate phase-space coupling and avoid spin rotation in the case of polarized beams. The field strengths are adjusted such that $\int B \cdot dl$ over the cooler magnets and the compensating solenoids equals zero. The main drift solenoid was typically operated at magnetic fields of B = 50-80 mT.

TABLE II. Parameters of the electron cooler at COS	Y [•	42]	•
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Electron cooler				
Electron energy	20-100 keV			
Typical electron beam current	0.25 A			
Magnetic field strength	50–150 mT			
Length of drift solenoid	2.00 m			
Bending radius in the toroids	0.60 m			
Effective length of cooling	1.50 m			
Effective length of solenoidal field	3.20 m			
Effective length of compensation	0.5 m			
Solenoids				
Diameter of COSY beam tube	0.15 m			
Diameter of electron beam	0.025 m			
Typical β -functions at the e-cooler	$\beta_x = 6 \text{ m}, \beta_y = 20 \text{ m}$			
Diagnosis	H ⁰ profile monitor			
-	and count rate			

Beams of small emittance, as produced by electron cooling, tend to develop coherent betatron oscillations which lead to beam loss [42]. The transverse feedback system of COSY [44,45] was used to avoid these instabilities.

B. Low- β insertion

In a storage ring, the geometrical machine acceptance¹ [41] is defined by

$$A_{x,y} = \left(\frac{a_{x,y}^2}{\beta_{x,y}}\right)_{\min},\tag{6}$$

and the acceptance angle Θ_{acc} [46], by

$$\frac{1}{\Theta_{\rm acc}^2} = \frac{1}{2\Theta_x^2} + \frac{1}{2\Theta_y^2} \quad \text{with} \quad \frac{1}{\Theta_{x,y}^2} = \frac{\beta_{x,y}}{A_{x,y}}, \tag{7}$$

where x and y indicate the horizontal and vertical direction, respectively, and a is the free aperture along the ring. At the kinetic energy of $T_p = 49.3$ MeV of the spin-filtering experiment, the beam lifetime [see (3)] is dominated by the Coulomb scattering loss on the target gas and the residual gas in the ring; the hadronic losses amount to about 10% of the total loss cross section σ_b (see Sec. VIII B). The Coulomb-loss cross section can be derived by integration of the differential Rutherford cross section for scattering angles larger than Θ_{acc} [47],

$$\sigma_C = \int_{\Theta_{\rm acc}}^{\Theta_{\rm max}} \int_0^{2\pi} \frac{d\sigma}{d\Omega} d\phi \sin \Theta d\Theta = 4\pi \frac{Z_{\rm gas}^2 Z_i^2 r_i^2}{\beta_L^4 \gamma_L^2} \cdot \frac{1}{\Theta_{\rm acc}^2}.$$
(8)

 Z_{gas} and Z_i are the atomic numbers of the target (or residual) gas and the ion beam, respectively, β_L and γ_L are the relativistic Lorentz factors, and $r_i = r_e m_e/m_i$ is the classical ion radius. The beam lifetime due to single Coulomb scattering,

$$\tau_b \approx \tau_C = \frac{1}{\sigma_C d_t f} = \frac{\beta_L^4 \gamma_L^2}{4\pi Z_{\text{gas}}^2 Z_i^2 r_i^2} \cdot \frac{\Theta_{\text{acc}}^2}{d_t \cdot f} \propto \frac{1}{d_t \cdot \beta}, \qquad (9)$$

is inversely proportional to the β -function and the gas density. Therefore, especially the β -functions at the PAX-TP should be small, because of the high densities.

It turns out that for a given target-gas cell there is an optimal value for the β -function at the cell center. The β -function in a symmetric drift space is described by

$$\beta(s') = \beta_0 + \frac{s'^2}{\beta_0},$$
 (10)

where $s' = s - s_0$ is the distance from the cell center s_0 and β_0 is the β -function at the center. The machine acceptance for a storage cell of diameter *d* and length *l* as a function of β_0 is therefore given by

$$A(\beta_0) = \frac{(d/2)^2}{\beta_0 + \frac{(l/2)^2}{\beta_0}},\tag{11}$$

and $A(\beta_0)$ reaches a maximum for $\beta_0 = l/2$. A storage cell of $d=9.6 \,\mathrm{mm}$ and $l=400 \,\mathrm{mm}$ is used to maximize the target areal density in the experiment (see Sec. III A). For the specified cell the maximum acceptance is $A(\beta_0 =$ $0.2 \,\mathrm{m}) \approx 58 \,\mu\mathrm{m}$ (see Fig. 3). The standard COSY lattice $(D \neq 0)$ provides geometrical acceptances of about $A_x \approx$ $(75 \,\mathrm{mm})^2/25 \,\mathrm{m} = 225 \,\mu\mathrm{m}$ and $A_y \approx (30 \,\mathrm{mm})^2/20 \,\mathrm{m} =$ $45 \,\mu\mathrm{m}$ (see Fig. 2 and Table I), thus with the smallest



FIG. 3. Machine acceptance $A(\beta_0)$ using (11) for a storage cell with diameter d = 9.6 mm and length l = 400 mm as a function of β_0 at the target center. A reaches a maximum for $\beta_0 = l/2 = 0.2$ m.

¹Throughout this paper μ m is used as a unit of machine acceptance and beam emittance, equivalent to mm mrad.



FIG. 4. View of the PAX installation at COSY from the interior of the ring (the beam comes from the left). 1: COSY quadrupole magnet; 2: two of the four PAX quadrupoles (formerly used at CELSIUS [48]) forming the low- β insertion by doublet focusing (DF-FD); 3: atomic beam source (ABS); 4: support system; 5: flange supporting rail system; 6: PAX target chamber housing the storage cell. The Breit-Rabi polarimeter (BRP) and the target-gas analyzer (TGA) are mounted towards the outside of the ring. The horizontal distance between the inner faces of the two COSY quadrupole magnets is 3.75 m, the height of the beam-tube center from the ground is 1.80 m.

 β -functions of about 3 m, the given storage cell would restrict the machine acceptance to $A(\beta_0=3 \text{ m}) \approx 8 \mu \text{m}$.

To obtain the required small β -functions, a low- β insertion consisting of four additional quadrupole magnets (blue in Fig. 4), formerly used at CELSIUS [48], was installed in the drift space in front of and behind the target. The quadrupole magnets are arranged in a doublet structure (DF-FD), where the *D* and *F* magnets are powered by separate power supplies. When the doublets are operated, the four regular COSY quadrupole families in this straight section are reduced in strength to maintain its telescopic nature. Thus the other magnets in the machine do not require any readjustment.

Precise positioning of the beam inside the storage cell was provided by horizontal and vertical steerer coils, which because of space restrictions were mounted on the yokes of the adjacent quadrupole magnets upstream and downstream of the low- β insertion.

Based on the COSY lattice using the standard magnet settings, the optical functions were calculated with the methodical accelerator design (MAD) program, version 8 [49]. The results obtained with the PAX magnets switched ON and OFF are shown in Fig. 5, indicating that β_x and β_y at the target point can be reduced by more than 1 order of magnitude, with minimal values of $\beta_{x,y} \approx 0.3$ m. The commissioning of the low- β section, including the measurement of β_x and β_y , is described in Sec. VI.

Reduced β -functions at the target, however, are accompanied by increased β -functions up- and downstream, reaching values of about 33 m (see Fig. 5, bottom panel).

Therefore, excellent vacuum conditions also have to be maintained in these regions to avoid adversely affecting the beam lifetime.

III. POLARIZED TARGET

A. Polarized atomic beam source and storage cell

The polarized internal target (PIT) consists of the atomic beam source (ABS), which was developed for the TSR spin-filtering experiment [9,50], later used in the HERMES experiment at DESY [51,52] and now modified for spinfiltering at COSY, a storage cell [53], a Breit-Rabi polarimeter (BRP) [54], and a target gas analyzer (TGA) [55]. H⁰ atoms in a single hyperfine state are prepared in the ABS and injected into a thin-walled storage cell. A fraction of the gas diffuses from the cell through a side tube into the diagnostic system, where the BRP determines the atomic polarization and the TGA the relative fraction of atoms and molecules. A magnetic guide-field system defines the quantization axis for the target polarization, which can be oriented along the *x* (outward), *y* (up), or *s* (along beam) direction, or any superposition thereof (see Sec. III B).

The gas load into the target chamber and the neighboring sections causes beam losses due to the interaction of beam particles with the residual gas. A dedicated pumping system, described in Sec. III C, was developed to minimize these losses.

The storage cell (see Fig. 6, label 1) increases the dwell time of the polarized atomic gas in the interaction region with the beam and enhances the areal target density



FIG. 5. Model calculation of the β -functions for the standard COSY setting $(D \neq 0)$ with PAX magnets switched OFF (top panel) and ON (bottom panel), indicating that minimal values of $\beta_{x,y} \approx 0.3$ m can be reached at the target point at s = 19.87 m. s = 0 is located at the beginning of the target straight section.

compared to a free atomic jet by about 2 orders in magnitude. The cell was made from aluminum and coated with Teflon² to reduce depolarization and recombination [56]. Assuming linear decrease of the gas density from the center to the open ends, the areal target-gas density is given by

$$d_t = \frac{1}{2} \cdot \frac{l \cdot I}{C_{\text{tot}}},\tag{12}$$

where $I[s^{-1}]$ is the intensity of the injected beam from the ABS, l[cm] the total length of the storage tube, and C_{tot} the total conductance of the storage cell. The conductance $[\ell/s]$ of a circular tube of diameter d_i [cm] and length l_i [cm] can be written as [57]



FIG. 6. Section view of the PAX target chamber. The labels denote the storage cell (1) with feeding tube to the ABS (vertical), and extraction tube to the BRP (to the backside), flow limiters (2) of 19 mm diameter and 80 mm length, jalousie (3) to protect the cell from heat radiation during activation of the nonevaporable getter (NEG) pumps (4), COSY beam (5), guide field compensation coils (6), and magnetic guide field coils (7).

$$C_i = 3.81 \sqrt{\frac{T}{M}} \cdot \frac{d_i^3}{l_i + 1.33 \cdot d_i},\tag{13}$$

where T [K] is the temperature and M [u] the molar mass.

The total conductance C_{tot} of the storage cell is given by the sum of all conductances with respect to the cell center. For a storage-cell tube (l = 400 mm, d = 9.6 mm), a feeding tube from the ABS (l = 100 mm, d = 9.6 mm), and the extraction tube to the target polarimeter (l = 380 mm, d = 9.6 mm), the conductance of the storage cell yields $C_{\text{tot}} = 2 \cdot C_{\frac{1}{2}\text{cell}} + C_{\text{feed}} + C_{\text{extract}} = 12.15\ell/\text{s}$. With an intensity from the ABS injected into the feeding tube of $I = 3.3 \times 10^{16} \text{ s}^{-1}$ [51], an areal density of $d_t =$ $5.45 \times 10^{13} \text{ cm}^{-2}$ is expected. During the spin-filtering experiment, in good agreement with the estimate given above, a target density of [28]

$$d_t = (5.5 \pm 0.2) \times 10^{13} \text{ cm}^{-2},$$
 (14)

was deduced from the shift of the orbit frequency of the coasting beam caused by the energy loss in the target gas (see Sec. IV B) [8,58].

B. Holding field coil system

The operation of the polarized target requires a coil system providing guide fields of about 1 mT [59] in order to define the orientation of the target polarization and allowing it to be reversed in short sequence. The polarization of the gas atoms is known to be fully reversed within

²Teflon (polytetrafluoroethylene) coating was done by Rhenotherm, Kunststoffbeschichtungs GmbH, Kempen, Germany.



FIG. 7. Calculated vertical magnetic flux density B_y along the s'-direction for the coil configuration of Fig. 6. In the target cell region (s' = -200 mm to +200 mm), indicated by the vertical dashed bars, the magnetic field is about 1 mT.

about 10 ms after switching the polarity of the magnetic field (see Fig. 11 of [60]). A system of coils, providing fields in transverse (x, y) and longitudinal (s) directions, was installed on the target chamber (see Fig. 6).

Additional coils installed on the up- and downstream ends of the target chamber (see Fig. 6) made sure that the horizontal and sideways field integrals $\int B_{x,y} ds$ vanish (see Fig. 7), thereby preventing the beam positions in the rest of the machine from being affected. Holding field and compensation coils require only a single power supply.

A measurement of the magnetic field B_y in the center of the target chamber using a Hall probe yielded $B_{y\downarrow} =$ -1.08 ± 0.03 mT and $B_{y\uparrow} = 1.10 \pm 0.03$ mT, pointing downward and upward, respectively. This result is in good agreement with the calculated magnetic field of 1.0 to 1.1 mT inside the storage cell based on the coil geometry shown in Fig. 6, using the Amperes [61] program.

The vertical magnetic guide field causes a deflection of the proton beam in the horizontal direction. According to $\vec{F}_x = q(\vec{v}_s \times \vec{B}_y)$, for a beam at experiment energy the expected change of the beam position at the target center between the two polarities ($B_y = \pm 1 \text{ mT}$) is $\Delta x \approx$ 0.28 mm. A measurement of the beam displacement using the movable frame system (see Sec. IV D) resulted in $\Delta x = x_{B_{y\uparrow}} - x_{B_{y\downarrow}} = (0.33 \pm 0.04) \text{ mm}$, confirming independently the magnetic holding field strength of $|B_{y\uparrow,\downarrow}| \approx 1 \text{ mT}$.

The quality of the magnetic compensation scheme was determined using the dispersion-free setting (D = 0) of the telescopes by measuring the horizontal orbit difference $\Delta x = x_{B_{y\uparrow}} - x_{B_{y\downarrow}}$ for reversed vertical magnetic holding fields $(B_{y\uparrow} \text{ and } B_{y\downarrow})$ using the beam position monitors (see Sec. IV). Small orbit differences in the arcs of $\Delta x \leq 0.9$ mm and in the straight sections of $\Delta x \leq 0.2$ mm were



FIG. 8. Difference of the horizontal orbit position $\Delta x = x_{B_y\uparrow} - x_{B_y\downarrow}$ along COSY for reversed vertical holding fields.

observed (see Fig. 8), yielding satisfactory stability of the beam position in the machine.

The largest orbit displacements occur in the arcs, where the dispersion reaches values of $D \approx 15$ m (see Fig. 2, bottom panel). It is interesting to note that according to (5) the observed orbit difference in the arcs apparently corresponds to a relative momentum change of $|\Delta p/p| \approx 10^{-5}$, which is probably due to a change of the proton-beam position inside the electron cooler beam when the magnetic holding field changes from $B_{v\uparrow}$ to $B_{v\perp}$.

C. Vacuum system around the target

The atomic beam source injected about $3.3 \times 10^{16} \text{ H}^{0}/\text{s}$ (one hyperfine state) into the target chamber, thus generating a significant gas load in the region around the PAX target. In the up- and downstream areas where the betatron functions are large (see Sec. IIB), and therefore the acceptance angles are small, single scattering on the residual gas causes beam losses that limit the beam lifetime. In order to minimize these losses, a complex vacuum system was installed. It consists of (i) ten NEG cartridges³ installed below the target chamber, providing a nominal pumping speed of $10 \times 1900 \ell/s$ for H₂ (see Fig. 6); (ii) NEG coating of the beam pipes up- and downstream of the target region with a nominal pumping speed of $2 \times 5000 \ \ell/s$ [62]; (iii) flow limiters with an inner diameter of 19 mm and a length of 80 mm (see Fig. 6) installed at the entrance and exit of the target chamber in order to minimize the gas flow from the target into the adjacent sections without restricting the machine acceptance; and (iv) one

³SAES getter pump GP 500 MK5, a type of vacuum pump manufactured by SAES GETTERS (Deutschland) GmbH, Cologne, Germany, sorbs active gases with a nonevaporable getter (NEG) material (Zr-V-Fe alloy).

turbo pump⁴ with a nominal pumping speed of 1200 ℓ/s for H₂ installed below the target chamber, primarily used during the activation of the NEG pumps.

The NEG coating and the NEG cartridges were activated by heating to 230 °C and 450 °C, respectively, exploiting the fact that the entire low- β section is bakeable. Assuming a gas flow of about 3.3×10^{16} H⁰/s during operation of the target, approximately one activation per week is required. A jalousie with mirror plates is mounted above the NEG cartridges in order to minimize the heat radiation into the target chamber during activation. The jalousie is closed during heating and opened for pumping. In addition, fast closing valves⁵ were installed at the up- and downstream ends of the target chamber, which are capable of sealing the section off from the rest of the ring during bakeout, or in case of a sudden vacuum break.

The vacuum system enabled a base pressure of 2×10^{-10} mbar in the target chamber and less than 10^{-11} mbar in the adjacent sections when the polarized target is switched off. During operation of the polarized target the pressure never exceeded about 10^{-7} mbar in the target chamber and 10^{-9} mbar in the adjacent NEG-coated vacuum tubes.

IV. BEAM DIAGNOSTIC TOOLS

Various beam diagnostics systems available at COSY were used to perform the studies described in this paper.

A. Beam current transformer

A beam current transformer (BCT) measures the current of the circulating ion beam. The BCT electronics are based on the DCCT principle (DC current transformer) [63] and can be set to deliver 1 V or alternatively 0.1 V output signal for 1 mA of beam current. The BCT signal forms the basis for the measurement of the beam lifetime, which was determined from a continuous record of the beam current as function of time, fitted by an exponential.

B. Beam position monitors

The beam position monitors (BPMs) at COSY are of the electrostatic type. Each BPM consists of two pairs of electrodes, providing sensitivity along the x and y direction. The electrodes, diagonally cut from a cylindrical or rectangular stainless steel tube, are matched to the size of the beam tubes in the straight and arc sections (see Table I) [64].

A bunch of charged particles passing through the device induces a voltage change that depends on the distance of the beam to the electrodes. The voltage difference at the two electrodes $\Delta = U_1 - U_2$ divided by the voltage sum $\sum = U_1 + U_2$ determines the beam position. A Fourier analysis of Δ as a function of time allows the transverse Fourier components of the beam spectrum to be extracted, which are used to determine the betatron tunes Q_x and Q_y (described in more detail in Sec. VA).

The sum signal \sum recorded with an unbunched beam was used to determine the longitudinal Fourier components of the beam spectrum, from which the revolution frequency *f* and the momentum spread Δp were obtained.

The beam-energy loss, caused by the interaction of the beam with the residual gas in the machine and the target gas, leads to a change of the revolution frequency per unit of time and is used to determine the target density (see (7) of [58]).

C. Stripline unit

The stripline unit of COSY uses four electrodes mounted azimuthally at 45° with respect to the *x* and *y* direction to excite coherent betatron oscillations [65]. The unit is powered with a frequency-swept sine wave voltage. The coherent betatron oscillations of the beam as a function of the exciting frequency are recorded with a BPM and Fourier analyzed to yield the fractional betatron tune, as described in Sec. VA.

D. Movable frame system

A frame system was installed at the PAX target position consisting of three frames and a tube (see Fig. 9) [66]. The widths of each frame were determined with a precision of 1 μ m by a coordinate measuring machine. The machine acceptance angles Θ_x and Θ_y at the upstream end, the center, and the downstream end of the storage cell were determined with the beam passing through one of the orifices by moving the system along the *x* or the *y* direction and by simultaneously measuring the beam lifetime (see Sec. VII C). The tube was utilized to precisely align the proton beam at the target prior to the installation of the storage cell.

E. Ionization profile monitor

An ionization profile monitor (IPM), developed in cooperation with the Gesellschaft für Schwerionenforschung mbH, Darmstadt, Germany (GSI), provides a fast and reliable nondestructive beam profile and position measurement [67]. The interaction of the stored beam with the residual gas produces ions which are guided to a positionsensitive detector by transverse electric fields. The ion detection is based on an arrangement consisting of microchannel plates, where secondary electrons are produced, a phosphor screen to produce light, and a CCD camera to detect the light. The system enables a continuous recording of the beamwidth during the cycle with a resolution of 0.1 mm [68]. The measured distribution of ions is fitted by a

⁴A HiPace 1800 turbo pump from Pfeiffer Vacuum GmbH, Asslar, Germany was used.

⁵The fast closing valves of series 750: DN-100-CF were manufactured by VAT Deutschland GmbH, Grasbrunn, Germany.



FIG. 9. Movable system with three frames of orifice cross section $w_x \times w_y \approx 25 \text{ mm} \times 20 \text{ mm}$, at the upstream (2), center (1), and downstream position (3) of the storage cell, and one tube of 9.6 mm inner diameter and 400 mm length. The system is movable in the horizontal (*x*) and vertical (*y*) direction perpendicular to the beam while the beam passes through one of the apertures.

Gaussian (see Fig. 10). The resulting beamwidths $2\sigma_{x,y}$ are used to calculate the 2σ beam emittances,

$$\epsilon_{x,y} = \frac{(2\sigma_{x,y})^2}{\beta_{x,y}},\tag{15}$$

where $\beta_{x,y}$ represent the β -functions in the horizontal (*x*) and vertical (*y*) plane at the location of the IPM.

F. H⁰ monitor

A small fraction of protons and electrons recombines in the electron cooler to neutral H^0 atoms, which are not



FIG. 10. Beam profile measurement in the horizontal plane using the ionization profile monitor. Fitting the particle distribution by a Gaussian provides the beamwidth.

deflected in the magnetic elements. The H^0 monitor [69], located at the end of the cooler straight section, records the H^0 beam profile using a multiwire proportional chamber, while scintillators are used to determine the intensity of the H^0 beam. In particular, the H^0 beam intensity provides an indispensable tool to properly set up the electron cooler and to monitor its performance.

G. Beam polarimeter (ANKE)

The beam polarization after spin filtering was measured using $\vec{p}d$ elastic scattering, described in detail in [10,28]. The ANKE deuterium cluster-jet target [70] provides target densities of about 1.5×10^{14} deuterons per cm². Elastically scattered particles were detected in the silicon tracking telescopes [71] located left and right of the cluster target at the ANKE interaction point (see Fig. 1), allowing the determination of the beam polarization from the measured left-right asymmetry and the analyzing power of $\vec{p}d$ elastic scattering [29].

V. BETATRON TUNE AND ORBIT ADJUSTMENT

Before actual commissioning of the low- β section, suitable betatron tune settings and corrections to the machine orbit had to be carried out in order to provide good starting conditions for further optimization of the machine with respect to the beam lifetime (Sec. VA).

In the following section, in particular, the mapping of the betatron tunes under different conditions and the coupling of the horizontal and vertical phase space are discussed. The implemented closed orbit correction procedures aimed at a reduction of the local acceptance limitations in the machine in order to optimize the beam lifetime (Sec. V B).

A. Betatron tune mapping

The particles circulating in COSY with frequency f perform betatron oscillations in the horizontal (x) and vertical (y) plane which are induced by the focusing strength of the quadrupole magnets in the ring. To first order the betatron motion constitutes a sinusoidal wave with frequency $f_{\beta_{x,y}} = f \cdot Q_{x,y}$, where $Q_{x,y}$ denotes the betatron tunes (or working point). The number of betatron oscillations per turn is given by

$$Q_{x,y} = \frac{\Delta \psi_{x,y}}{2\pi} = \frac{1}{2\pi} \oint \frac{ds}{\beta_{x,y}(s)}.$$
 (16)

Here $\Delta \psi_{x,y} = \psi_{x,y}(s+C) - \psi_{x,y}(s)$ is the phase change per revolution, and *C* the ring circumference.

At COSY, in order to analyze the betatron tune of the machine, a network analyzer is used to induce coherent transverse betatron oscillations of the beam by powering the stripline unit (see Sec. IV C) with a frequency-swept sine wave voltage, covering the frequency range of a

series of lower (-) and upper (+) betatron sidebands at

each revolution harmonic n with center frequencies of

$$f_{-} = (n - q_{x,y})f$$
 and $f_{+} = (n + q_{x,y})f$, (17)

where f denotes the average revolution frequency. Since the betatron motion is sampled by the pickup once per turn, the measured spectrum provides only information about the fractional tune $q_{x,y} = \operatorname{frac}(Q_{x,y})$, where $Q_{x,y} = \operatorname{int}(Q_{x,y}) + q_{x,y}$. The fractional tune is deduced from the peak value of both sideband frequencies, and the revolution frequency is found by adding them up. Inserting the resulting value for f into (17) yields q_x and q_y .

Because of the symmetry in a synchrotron such as COSY, the magnetic structure after each full turn merges into itself. Consequently, the forces on the beam recur periodically, and, therefore, the betatron tunes should be irrational numbers in order to avoid betatron resonances that can lead to an expansion of the beam or even to beam loss. The resonance condition is given by

$$mQ_x \pm nQ_y = l, \qquad m, n, l \in \mathbb{N}.$$
(18)

In order to increase the beam lifetime, a search for the optimal betatron tunes was performed for several machine settings, and, to this end, different tune combinations (Q_x, Q_y) were investigated. In this procedure, called tune mapping, the currents in the quadrupole magnet families QU1-3-5 and QU2-4-6 were varied in the range of $\pm 3\%$, while the beam lifetime was determined from an exponential fit to the beam current using the BCT signal (see Sec. IVA).

The betatron tune scans, carried out with $D \neq 0$ setting of COSY, showed a large variation in the beam lifetime by a factor of 6 in a rather small region of betatron tunes (see Fig. 11). Maximum beam lifetimes were observed close to the standard COSY working point of $Q_x = 3.58$ and $Q_y = 3.62$. This is in good agreement with tracking calculations carried out for COSY using MAD-X [49]. The impact of the third and sixth order machine resonances on the beam lifetime is clearly visible, as shown in Fig. 12.

An early investigation of the COSY beam lifetime as a function of the betatron tunes (Q_x, Q_y) confirmed that the beam lifetime increased with decreasing tune split $\Delta Q^{\text{split}} = Q_x - Q_y$ (see Fig. 11), as mentioned in [72]. Coupling between the horizontal and vertical betatron oscillations leads to a rotation of the eigenvectors of the transverse oscillations, thus the difference resonance $\Delta Q^{\text{split}} = 0$ cannot be reached. Betatron motions can be coupled through solenoidal and skew-quadrupole fields. The latter arise, for instance, from quadrupole rolls and feed-downs from higher-order multipoles caused by an



FIG. 11. Beam lifetime as a function of the working point (Q_x, Q_y) . While the beam lifetime increases with decreasing distance to the difference tune $Q_x = Q_y$ (dashed line), $\Delta Q^{\text{split}} = 0$, cannot, however, be achieved because of coupling.

off-axis beam orbit [73]. The observed tune split $\Delta Q^{\text{split}} = 0.014$ (shown in Fig. 12) cannot be attributed to phase-space coupling induced by the main solenoid and the two compensation solenoids of the electron cooler, because they were operated in compensation mode (see Sec. II A).

Applying additional corrections by using the COSY sextupole magnets of proper polarity led to a reduced coupling and yielded $\Delta Q^{\text{split}} \approx 0.006$. The seven additional data points originating from this correction are shown in the central corridor in Fig. 12. This indicated that the coupling might originate from sextupole components in the fields of the dipole magnets which affect the beam in an off-axis position. This conclusion was confirmed in later



FIG. 12. Beam lifetime as a function of the betatron tunes Q_x and Q_y . The data from Fig. 11 are shown here again together with additional data points in the central region close to $Q_x = Q_y$ (low coupling), which were obtained by an adjustment of sextupole magnets. The dashed lines correspond to $|\Delta Q^{\text{split}}| = 0.014$. Sum and difference resonances of the second, third, and sixth order are shown, representing the strongest multipole components of dipole and quadrupole magnets in the machine.

measurements, performed to commission the low- β insertion (see Fig. 15), which showed that a comparably small ΔQ^{split} could be reached without sextupole corrections by applying instead a closed orbit correction. An independent measurement at COSY with a 232.8 MeV deuteron beam [74] arrived at the same conclusion. Starting with a distorted orbit at the acceptance limit yielded $\Delta Q^{\text{split}} = 0.011$, and by applying a careful closed orbit correction, the coupling was decreased by about a factor of 4 to $\Delta Q^{\text{split}} = 0.003$.

The achieved tune splits correspond to a small linear coupling in the machine, which is neglected in later considerations.

B. Closed orbit correction

Due to misalignment or field errors of magnets, the real orbit in a machine deviates from the ideal one. In regions where the β -functions are large, these deviations lead to local restrictions of the machine aperture and thus reduce the lifetime of the beam. A closed orbit correction scheme, based on the orbit response matrix (ORM), was implemented to increase the machine acceptance and to improve the beam lifetime [75,76]. In addition, the orbit correction allows one to specify boundary conditions such as the beam position at the target or the electron cooler.

The entries $R_{s,i}^u$ of the ORM reflect changes of the orbit deviation u(s) (u = x or y) measured with a BPM at a position s in the ring, which is caused by a change in the deflection strength $\Theta_u(i)$ of a correction-dipole magnet at a position i affecting the beam in the horizontal (u = x) or vertical (u = y) direction. For x or y these quantities are connected by the relation

$$u(s) = R^u_{s,i} \cdot \Theta_u(i), \tag{19}$$

where

$$R_{s,i}^{u} = \sqrt{\beta_{u,i}\beta_{u,s}} \cdot \frac{\cos(\pi Q_u - \psi_{u,s \to i})}{2\sin(\pi Q_u)}$$
(20)

depends on the transverse tune Q_u , on the β -function at the beam position monitors and correction-dipole magnets, and on the phase advance between the positions *s* and *i*, denoted by $\psi_{u,s\to i}$. The ORM can either be calculated for the beam optics of the ring or measured. Here, the latter method was applied. When M horizontal (*x*) and vertical (*y*) BPMs and N_x and N_y correcting elements are installed, then (19) is replaced by

$$\vec{u} = R^u \cdot \vec{\Theta}_u, \tag{21}$$

where $\vec{\Theta}_u$ is a vector of N_x or N_y components, \vec{u} is a vector of M components, and R^u is a $M \times N_x$ or $M \times N_y$ matrix with the calculated elements $R_{s,i}^u$.

For $M \ge N_x, N_y$, which was fulfilled in the present studies, the horizontal and vertical closed orbit corrections were derived by varying the $\Theta_u(i)$ kick angles to find the minimum quadratic residual $|R^u \cdot \vec{\Theta}_u - \vec{u}|^2$ [75–77]. This method was also used in the present studies. Another possibility uses the inversion of the ORM, where the appropriate settings are calculated from $\vec{\Theta}_u = R^{-1}\vec{u}$. This method is usually faster, though it should be noted that an inversion of the matrix *R* is not always possible.

The closed orbit correction procedure for COSY was tested for the first time in January 2009 within the framework of a PAX beam time and has been further optimized since then with the aim of achieving longer beam lifetimes at injection energy. The measurement of the ORM made use of up to $N_v = 17$ vertical orbit correction dipole magnets for the measurement of the vertical ORM. 20 horizontal orbit correction dipole magnets, two horizontal back-leg windings at the ANKE dipole magnets, and both compensation dipole magnets next to the electron cooler toroid magnets were used for the determination of the horizontal ORM, i.e., $N_x = 24$. Depending on their availability, up to M = 31 beam position monitors were employed. The $M \ge N_x$, N_y required above was always fulfilled. Phase-space coupling was neglected in these measurements. The beam was deflected in both transverse planes by changing the current of a particular correction dipole magnet by about 5%. The orbit changes at the BPMs, normalized to the variation of the current, correspond to the entries of the ORM. In spite of the longer computation time, a χ^2 minimization was used to determine the correction angle kicks $\tilde{\Theta}_{u}(i)$.

A typical example of a closed orbit correction with two iterations is shown in Fig. 13. The vertical COSY orbit displays smaller deviations than the horizontal one. For the horizontal orbit correction, the initial deviations of up to 35 mm were decreased to less than 10 mm. Recent studies, carried out in 2011, show that with the presently available instrumentation at COSY the limit of the orbit correction procedure is $\Delta x = \Delta y \approx 3$ mm.

VI. COMMISSIONING OF LOW-β INSERTION

Prior to the polarization buildup measurements, the low- β insertion (see Sec. II B) was commissioned in a dedicated beam time. The aim was to achieve betatron amplitudes at the target center of about $\beta_{x,y} \approx 0.3$ m without significant reduction of the beam lifetime. MAD calculations [49] verified that the PAX low- β quadrupoles have to provide 10 to 40 times larger focusing strengths than the regular COSY quadrupole magnets in order to achieve the required small β -functions at the target. Horizontal or vertical displacements of the beam in the strong low- β magnets would cause large orbit excursions along the ring. Therefore, a careful closed orbit correction (see Sec. V B) and selection of a reasonable working point (see Sec. VA) were carried out



FIG. 13. Effect of horizontal (top) and vertical (bottom) closed

orbit correction for COSY at injection energy ($T_p = 45$ MeV).

The initial vertical orbit deviations are in general smaller than the

prior to the commissioning to avoid beam losses when the

taining the telescopic features of the straight section was

accomplished using as a starting point a regular COSY

optics setting at $T_p = 45$ MeV, with dispersion $D \neq 0$ and

low- β section switched off. Subsequently, the fields of the

low- β quadrupole magnets were increased in strength

stepwise, while those of the COSY quadrupoles in the

same straight section were reduced in strength such that

the betatron tunes remained constant. Figure 14 shows the

current in the COSY quadrupole families QT1-QT4 vs the

current in the PAX low- β magnets found in this process.

The MAD model was used to calculate the β -function at the

center point of the insertion (see Fig. 14, right scale). The

strengths of the low- β PAX quadrupole magnets were

reduced in the calculation by an empirical value of 4%

to achieve stable solutions in the lattice calculations.

The goal of operating the low- β insertion while main-

low- β quadrupole magnets are operated.

horizontal ones.

In

β-fun

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FIG. 14. Currents in the COSY quadrupoles and the betatron amplitudes vs current of the PAX low- β quadrupoles. With increasing strength of the low- β magnets, the betatron amplitudes β_x (in blue) and β_y (in red)(right scale) decrease. The currents in the COSY quadrupoles (QT1-QT4) were reduced to keep the tune constant, using a $D \neq 0$ setting.

measuring the tune change of the machine. The quadrupole focusing strength $k = \frac{1}{B\rho} \frac{\partial B_y}{\partial x} = \frac{1}{B\rho} \frac{\partial B_x}{\partial y}$ is given by the magnetic rigidity $B\rho = 0.977$ Tm for the chosen kinetic energy of $T_p = 45$ MeV and the magnetic field gradient. The latter is expressed by $\frac{\partial B_y}{\partial x} = \frac{\partial B_x}{\partial y} = g \cdot I$, where g =0.0197 Tm⁻¹ A⁻¹ denotes the current-specific gradient and I is the operating current. The four PAX quadrupole magnets are powered pairwise. Therefore, the tunes are measured either as a function of the focusing strength, i.e., the operating current of the inner pair (PAX2, Fig. 15) or of the outer pair (PAX1). The current of the inner pair was modified in steps of 1 A from 181.4 to 199.4 A, corresponding to the range $k = 3.658 \text{ m}^{-2}$ to k =4.021 m⁻². The values for the outer pair are steps of 0.5 A from 181.7 to 188.2 A, corresponding to the range $k = 3.664 \text{ m}^{-2}$ to $k = 3.795 \text{ m}^{-2}$.

In Fig. 15 the measured tunes Q_x and Q_y are displayed as a function of the quadrupole strength of the outer pair (PAX1, bottom panel) and the inner pair (PAX2, top panel). According to [78], the functional form of $Q_{x,y}(k)$ is described by a hyperbola. The hyperbolic fits also yield the tune split of $\Delta Q^{\text{split}} = 0.0085 \pm 0.0010$, obtained from a weighted average using the outer and the inner quadrupole pair. This constitutes independent evidence for the presence of slight coupling in the machine, as already discussed in Sec. VA. The crossing points of the asymptotes at Q = 3.611 for the inner pair and Q = 3.613for the outer pair agree within the error of Q^{split} as expected.

The ion-optics matrix formalism for a change of the quadrupole focusing strength Δk yields a tune shift [41,79]

In order to verify the validity of the lattice model, the
$$\beta$$
-functions at the PAX quadrupoles were experimentally determined by changing the quadrupole strength and

 $\Delta Q_{x,y} = \frac{1}{4\pi} \int_{s_0}^{s_0+l} \Delta k \beta_{x,y}(s) ds,$ (22)



FIG. 15. Betatron tunes Q_x (horizontal) and Q_y (vertical) as a function of the focusing strength $k_{x,y}$ for the inner (top panel) and outer (bottom panel) pair of the PAX low- β quadrupoles. The data were fitted with a hyperbola, and the slopes of the asymptotes $|\Delta Q_{x,y}/\Delta k|$ were used to determine the β -functions. ΔQ^{split} is a measure of coupling in the machine.

where $\beta_{x,y}(s)$ is the position-dependent β -function and l is the effective length of the field of the quadrupole magnet. For small Δk , $\beta_{x,y}(s)$ can be replaced by $\overline{\beta}_{x,y}$, which yields

$$\bar{\beta}_{x,y} = \frac{4\pi}{l} \left| \frac{\Delta Q_{x,y}}{\Delta k} \right|. \tag{23}$$

The absolute value takes into account that the β -function has to be positive, remembering that a quadrupole focuses in one plane ($\Delta Q_{x,y} > 0$ for $\Delta k > 0$) and defocuses in the other plane ($\Delta Q_{y,x} < 0$ for $\Delta k > 0$). To determine the average values $\bar{\beta}_x$ and $\bar{\beta}_y$ in the magnets of the inner and outer pair using (23), the values of $|\Delta Q/\Delta k|$ are the absolute values of the four slopes of the asymptotes of the hyperbolas of Fig. 15. The effective length of a single PAX quadrupole magnet, measured as 0.442 m, for each of the pairs, yields l = 0.884 m. The resulting $\bar{\beta}_x$ and $\bar{\beta}_y$ are



FIG. 16. Model calculation of the β -functions at the PAX-TP and measured values of $\overline{\beta}_x$ and $\overline{\beta}_y$ at the magnet positions. The four new PAX quadrupole magnets are shown in blue. Magnets 1 and 4 form the defocusing (D) pair (PAX1) and magnets 2 and 3 the focusing (F) pair (PAX2), where each pair is operated with a single power supply. In addition, the storage cell and the beam direction are shown.

shown in Fig. 16 together with the result of the model calculation, which yields reasonable agreement (see Table III) with the measured data and $\beta_x = 0.31$ m and $\beta_y = 0.46$ m at the center of the target. From a comparison of measured and calculated betatron functions, an uncertainty of about 10% is estimated for the β -functions obtained from the MAD model.

VII. BEAM SIZE, BEAM EMITTANCE, MACHINE ACCEPTANCE, AND TARGET ACCEPTANCE ANGLE

The polarization buildup cross section $\tilde{\sigma}_1$ depends on the acceptance angle Θ_{acc} at the target location, as explained in Sec. I. Therefore, in order to determine $\tilde{\sigma}_1$, it is necessary to measure Θ_{acc} . The measurement made use of the fact that when an object is placed at a distance smaller than the maximum allowed extension of the local phase-space

TABLE III. Measured and calculated betatron functions β_x and β_y from the MAD model at the position of the PAX quadrupole magnets (outer pair: PAX1; inner pair: PAX2). The calculated β -functions at the target center are given in column six.

	Measurement		Model calculation		
	PAX1	PAX2	PAX1	PAX2	Center
β_x (m)	2.31 ± 0.13	2.80 ± 0.04	2.11	2.71	0.31
β_y (m)	12.41 ± 1.01	3.31 ± 0.05	12.99	2.74	0.46

ellipse, the machine acceptance is reduced, and therefore the beam lifetime as well [66,80].

In the subsequent section, we first describe the determination of the beamwidth at the target, since it may have some bearing on the machine acceptance extracted from a measurement with the scraper system, described in Sec. IV D. The actual acceptance measurements, including the determination of Θ_{acc} and a discussion of possible systematic errors, are discussed in Sec. VII C.

A. Measurement of the beamwidths at the target

The beamwidths along the PAX target were determined by moving each of the three rectangular frames (shown in Fig. 9) at constant speed through the proton beam. The decrease of the beam current was recorded with the BCT (see Sec. IVA). A typical result of such a frame scan is shown in Fig. 17. The remaining beam intensity as a function of the frame position is obtained by converting the measured time into the distance from the start position, using the constant velocity of the frame movement of

$$v_x = v_y = (1.65 \pm 0.02) \text{ mm/s}$$
 (24)

The measured beam profile constitutes half of an inverted Gaussian when the beam itself has a Gaussian profile [81]. Assuming no coupling in the machine (see Sec. VA), a scraper moving along the x (or y) direction removes only those particles from the (x, x') [or (y, y')] phase space for which the betatron amplitudes are larger than the distance from the beam center to the edge of the scraper (see Fig. 1 of [66]).



FIG. 17. Measured beam intensity as a function of frame position obtained by moving the frame through the beam. The resulting beam profile (black points) constitutes half of an inverted Gaussian from which σ as a measure of the beamwidth is obtained by fitting using (27) (dashed blue line). The beam intensity with the frame in the nominal position of $I_0 = 0.35$ mA corresponds to about 4.67×10^9 protons at injection energy.

A cooled and stored beam exhibits a two-dimensional Gaussian distribution in transverse phase space where the density distribution of the betatron amplitude ρ_{β} in e.g., the (x, x') plane [81,82] is given by

$$\rho_{\beta}(x) = \frac{I_0}{\sigma_x^2} \cdot x \cdot \exp\left(-\frac{x^2}{2\sigma_x^2}\right).$$
(25)

The measured beam intensity as a function of frame position can be written as [66]

$$I_{\text{frame}}(x) = \int_{0}^{x-\mu_{x}} \rho_{\beta}(x) \cdot dx = I_{0} \bigg[1 - \exp \bigg(-\frac{(x-\mu_{x})^{2}}{2\sigma_{x}^{2}} \bigg) \bigg].$$
(26)

Here I_0 is the beam intensity with the frame in the nominal position, μ_x is the beam center, and σ_x describes the beamwidth in the *x*-direction. Because the beam intensity decreases exponentially before intersecting the frame, the following function,

$$I(x) = I_{\text{frame}}(x) \cdot \exp\left(-\frac{x}{\tau_b \cdot v_x}\right), \quad (27)$$

was fitted to the measured beam intensity dependence, shown in Fig. 17, in order to determine σ_x and σ_y by the same procedure. Although with coupling or dispersion at the frame position, the functional form is more complicated [83], good agreement with the data was achieved using (27).

The beamwidths were determined for all three frames of the scraper system with the D = 0 setting (see Sec. II A) at $T_p = 45$ MeV. Horizontally, the frames could be moved in the positive and the negative direction, while vertical measurements were only feasible by moving the frames upward, because in the case of the downward movement the beam could not be completely removed due to space limitation.

The beamwidths $2\sigma_x$ and $2\sigma_y$ for each frame were determined by averaging the results of two independent measurements. In the case of the horizontal measurement, $2\sigma_x$ additionally includes averaging the results from both *x*-direction measurements. The results are listed in Table IV. Unfortunately, the vertical measurement at the target center (s' = 0 mm) showed distortions that made the result inconsistent. The measurements confirm that the beamwidth $2\sigma_x$ is smallest at the cell center and, as expected knowing the β -functions, increases symmetrically toward the up- and downstream ends of the storage cell. The appropriate β -functions at the location of each frame were obtained from the validated MAD model (see Sec. VI) and are given in Table IV.

TABLE IV. Beam widths (in mm) determined at three positions, center (s' = 0 mm) and upstream (s' = -200 mm) and downstream (s' = +200 mm) ends of the PAX storage cell (see Fig. 9).

Frame	2	1	3
Position (s')	-200 mm	0 mm	+200 mm
$2\sigma_x$	1.04 ± 0.02	0.91 ± 0.04	1.04 ± 0.01
$2\sigma_v$	0.66 ± 0.02		0.67 ± 0.02
$\beta_x(\mathbf{m})$	0.62 ± 0.06	0.55 ± 0.06	0.62 ± 0.06
$\beta_y(\mathbf{m})$	0.48 ± 0.05	0.38 ± 0.04	0.48 ± 0.05

The averaged horizontal and vertical beamwidths are $2\sigma_x = 1.03 \pm 0.01$ mm and $2\sigma_y = 0.67 \pm 0.02$ mm. In terms of these beamwidths, the walls of the storage cell ($r_{cell} = 4.8$ mm) are at least 10 standard deviations away from the center of the beam.

B. Determination of the beam emittance

The values of the β -functions allow one to determine the 2σ beam emittance for each measurement from (15). Weighted averaging of the resulting three horizontal emittances yields

$$\epsilon_x = \frac{(2\sigma_x)^2}{\beta_x} = (1.71 \pm 0.17) \ \mu \text{m},$$
 (28)

and of the two vertical emittances yields

$$\epsilon_y = \frac{(2\sigma_y)^2}{\beta_y} = (0.92 \pm 0.15) \ \mu \text{m.}$$
 (29)

The given uncertainties arise from the uncertainty of the frame velocity, the statistical errors of the fit, and the estimated uncertainty of 10% on the β -functions, given in Table IV.

C. Determination of A_x , A_y , and Θ_{acc} at the target

The acceptance of a storage ring is defined in (6). At every point in the ring, the acceptance $A_{x,y}$ corresponds to a (horizontal and vertical) phase-space ellipse [73]. When at some point along the orbit, a restriction (frame) is moved into the machine acceptance, e.g., in the horizontal (*x*) direction, the maximum (*x*, *x'*) phase-space ellipse, representing the machine acceptance at that location, is intersected, and accordingly the beam lifetime is reduced (see Fig. 18). Every particle orbits on an individual phase-space ellipse in (*x*, *x'*) and (*y*, *y'*), and all ellipses at a specific location in the ring have the *same shape* [77]. While the insertion of the frame initially only presents a limitation of the *x* coordinate, because of the betatron motion, the *x'* coordinate is also affected. Therefore, the beam lifetime as a function of the frame position was measured in order to



FIG. 18. Horizontal phase-space distribution at the PAX target position from a Monte Carlo simulation. A typical machine acceptance at COSY ($A_x = 20 \ \mu m$, $A_y = 15 \ \mu m$) is indicated by the large ellipse. Moving a frame into the machine acceptance decreases both x and x', thus reducing the beam lifetime, and allowing A_x and Θ_x to be determined.

determine the machine acceptance and the acceptance angle at the target.

The total beam lifetime due to single Coulomb scattering is found to be [see (9) and (7)] [46]

$$\tau_b'(A_x, A_y) = c \cdot \Theta_{\rm acc}^2 = 2c \cdot \left(\frac{1}{\Theta_x^2} + \frac{1}{\Theta_y^2}\right)^{-1} = 2c \cdot \left(\frac{\langle \beta_x \rangle}{A_x} + \frac{\langle \beta_y \rangle}{A_y}\right)^{-1}, \quad (30)$$

where *c* is a constant during the measurement, $\langle \beta_x \rangle$ and $\langle \beta_y \rangle$ are, respectively, the average horizontal and vertical β -functions along the ring, and the *x*- and *y*-acceptance is either given by the ring acceptance $A_{x,y}^{\text{ring}}$ or the acceptance is defined by the frame position $A_{x,y}^{\text{frame}} = a_{x,y}^2 / \beta_{x,y}$ [see (6)], whichever is smaller. Here $a_{x,y}$ are the distances of the restriction to the beam center and $\beta_{x,y}$ are the β -functions at the location of the frame.

In the following, the acceptance measurement in the *x*-direction is exemplified (see Fig. 19). The measurement begins with the frame horizontally and vertically centered on the beam (x = 0). During the horizontal movement of the frame A_y is constant. As long as the frame does not limit the machine acceptance $(|x| \le |x_2|)$, the beam lifetime is not affected (part III in Fig. 19). When the frame moves into the machine acceptance $(|x_2| \le |x_2|)$, the beam lifetime beam lifetime become smaller (parts II and IV). When it reaches a position of $|x| \ge |x_1|$ the measured beam lifetime vanishes (parts I and V). Theoretically, the beam lifetime should vanish to zero when the frame reaches the center of the beam, corresponding to a position of $|x| = w_x/2$, where w_x is the measured frame width (see Sec. IV D).



FIG. 19. Schematic of the beam lifetime as a function of the position of the frame during an acceptance measurement. As long as the frame is outside the machine acceptance (part III), the beam lifetime is unchanged. When the frame limits the acceptance the beam lifetime drops (parts II and IV) according to (31), and when it intersects the beam itself, the beam lifetime vanishes (parts I and V). The acceptance is then defined by the frame width w_x and the position where the frame enters the machine acceptance x_2 .

Based on these considerations, the following fit function is formulated, using (30):

$$\tau_{b}(x) = \begin{cases} 0 & \text{if } x \leq -x_{1} & \text{I} \\ \tau_{b}'(A_{x}^{\text{frame}}, A_{y}^{\text{ring}}) & \text{if } -x_{1} \leq x \leq -x_{2} & \text{II} \\ \tau_{b}'(A_{x}^{\text{ring}}, A_{y}^{\text{ring}}) & \text{if } -x_{2} \leq x \leq x_{2} & \text{III} \\ \tau_{b}'(A_{x}^{\text{frame}}, A_{y}^{\text{ring}}) & \text{if } x_{2} \leq x \leq x_{1} & \text{IV} \\ 0 & \text{if } x \geq x_{1} & \text{V} \end{cases}$$
(31)

where A_y^{ring} , x_1 , and x_2 are fit parameters. The machine acceptance is determined from the distance between x_2 and the beam center by

$$A_x = \frac{(w_x/2 - x_2)^2}{\beta_x}.$$
 (32)

The offset of the beam with respect to the center of the frame can be determined with a typical uncertainty of 0.1 mm. For clarity, the offset parameter has been omitted in (31), but is taken into account in the actual fitting function.

Monte Carlo simulations of an acceptance measurement using realistic phase-space distributions at the PAX target position showed good agreement between simulated data and the fit function [see (31)] for typical beam sizes at the target (see Sec. VII A).

The acceptance measurements with the movable frame system (see Sec. IV D, Fig. 9) were carried out for all four

edges of each of the three rectangular frames. Moving each frame individually into the machine acceptance, while recording the beam lifetime, allowed one to determine the machine acceptance angles at the entrance of the storage cell (s' = -200 mm), at the center (s' = 0 mm), and at the exit (s' = +200 mm). A measurement carried out in the presence of the ANKE cluster target (see Sec. IV G) showed good agreement of the resulting acceptances.

The acquired data set enabled a precise determination of the machine acceptance, the acceptance angle in the horizontal and vertical direction, and of the total acceptance angle Θ_{acc} [see (7)] at the target. During the measurements, the beam intensity was in the range of $(7.5-10) \times 10^9$ circulating unpolarized cooled protons at the injection energy of 45 MeV, with the PAX low- β section switched on and an initial beam lifetime of about 3700 s.

During injection, the frame was horizontally and vertically centered on the beam. After injection and cooling, the frame was moved in the horizontal (vertical) direction and the resulting beam lifetime was recorded. An example of a measurement with frame 1, located at the target center, is shown in Fig. 20. The uncertainties of the beam lifetimes τ_b are of the order of 100 s, chosen to yield reduced χ^2 of approximately unity for the fits.

All fits indicate that the beam lifetime actually vanishes before the frame edge intersects the beam center. This is equivalent to stating that the observed width at the base $(\tau_b = 0)$ is smaller than the frame width (see Sec. IV D), thus $|x_1| + \delta_x = w_x/2$ and $|y_1| + \delta_y = w_y/2$ (see Fig. 20), where the discrepancy δ_x (δ_y) is of the order of $1.0 \pm$ 0.1 mm (0.5 ± 0.1 mm). Possibly, small beam oscillations of unknown origin are responsible for this observation. It should be noted that the approach of measuring the machine acceptance with a rectangular frame is sensitive to such effects, while this is not the case for a single-sided scraper measurement. Therefore, in the latter case, the machine acceptance might be underestimated.

The results for A_x , A_y , Θ_x , Θ_y , and Θ_{acc} using (6) and (7) are listed in Table V. The total acceptance angle at the target position amounts to

$$\Theta_{\rm acc} = (6.45 \pm 0.27) \,\,{\rm mrad.}$$
 (33)

The given uncertainty includes the error of the fit as well as an estimated 10% uncertainty of the β -functions.

The determined horizontal and vertical machine acceptances of $A_x = 31.2 \pm 2.5 \ \mu\text{m}$ and $A_y = 15.7 \pm 1.8 \ \mu\text{m}$ (see Table V) are significantly smaller than the simple geometrical acceptances estimated from the standard COSY lattice and the dimensions of the beam pipe (see Sec. II B). This is the case, because the beam lifetime is likewise impaired by dynamic effects through processes that act on long time scales, caused by nonlinear external fields [84]. Therefore, the method discussed here



FIG. 20. Recorded beam lifetime as a function of the horizontal (x, left panel) and vertical (y, right) position of frame 1 (PAX target center), and fit of $\tau_b(x)$ using (31). The fits indicate that the observed widths at the base ($\tau_b = 0$) were smaller than the corresponding frame widths (w_x, w_y), where the discrepancies $\delta_x = 1.0 \pm 0.1$ mm and $\delta_y = 0.5 \pm 0.1$ mm.

determines the relevant machine acceptance for spinfiltering experiments.

VIII. BEAM LIFETIME OPTIMIZATION

This section describes further machine investigations carried out at COSY aiming at an enlargement of the beam lifetime toward $\tau_b \approx 10000$ s, which is necessary to determine the spin-dependent cross section $\tilde{\sigma}_1$ of the polarization buildup during a few weeks of beam time. The starting point of the optimization is marked by a beam lifetime of $\tau_b = 800$ s, reached in 2007 for an electron-cooled proton beam at injection energy without a target [69].

Different processes contribute to the beam lifetime, such as betatron resonances, the Coulomb interaction with the residual gas and the target, intrabeam scattering, and hadronic interactions. Particle loss due to betatron resonances can be minimized by the choice of a suitable working point, also required for the commissioning of the low- β insertion (see Sec. VA). Coulomb interactions on the target and the residual gas comprise the following: (i) energy loss, causing particle losses at the longitudinal acceptance; (ii) emittance growth due to multiple smallangle scattering, causing losses at the transverse acceptance; and (iii) immediate loss of ions in a single collision where the scattering angle is larger than the transverse acceptance angle of the machine.

Energy loss and emittance growth can to a large extent be compensated by electron cooling (see Sec. II A). The beam lifetime due to single Coulomb losses was improved by the closed orbit correction procedure (see Sec. V B). Investigations of beam lifetime restrictions caused by spacecharge effects are discussed here in Sec. VIII A, while the contributions to beam lifetime from the residual gas in the machine and from the target are elucidated in Sec. VIII B.

A. Space-charge effects

When a machine is optimized for maximum beam lifetimes, space-charge effects as fundamental collective processes in beams of high intensity usually have to be considered. In the presence of electron cooling, where small emittances are achieved, space-charge effects are, however, already visible at low beam intensities.

TABLE V. Acceptance measurements with the movable frame system, listing the acceptances A_x and A_y , the acceptance angles Θ_x and Θ_y , and Θ_{acc} , using (6), (7), and the β -functions given in Table IV. One measurement with frame 1 was carried out with the cluster target switched on. The weighted averages are given in the bottom row. Results were rounded to one decimal place, while three decimal places were used for calculation and averaging.

Pos (m)	Frame	$A_x(\mu m)$	$A_y(\mu m)$	$\Theta_x(mrad)$	$\Theta_y(mrad)$	$\Theta_{\rm acc}({\rm mrad})$
-0.2	2	27.1 ± 4.0	16.8 ± 3.2	6.6 ± 0.6	5.9 ± 0.6	6.2 ± 0.4
0.0	1	49.7 ± 10.3	14.1 ± 6.0	9.5 ± 1.1	6.1 ± 1.3	7.3 ± 1.2
0.2	3	31.5 ± 4.7	19.6 ± 3.7	7.1 ± 0.6	6.4 ± 0.7	6.7 ± 0.5
0.0	1 (target on)	33.0 ± 5.1	12.4 ± 3.1	7.8 ± 0.7	5.7 ± 0.8	6.5 ± 0.6
Average		31.2 ± 2.5	15.7 ± 1.8	7.3 ± 0.3	6.0 ± 0.4	6.45 ± 0.27



FIG. 21. Widths 2σ from fits to beam profiles measured with the ionization profile monitor (IPM) vs the time after injection to COSY (< 25 s: electron cooling, 25–50 s tilting the electron beam with respect to the proton beam, > 50 s increased equilibrium beam size). The corresponding horizontal beam profile is shown in Fig. 10.

Studying space-charge effects and their impact on particle losses implies studying the effect of the beam emittance on the beam lifetime. For a constant beam intensity, the space charge decreases with increasing beam emittance. The beam emittance was manipulated by decreasing the cooling performance of the electron cooler. Both the horizontal and vertical electron beam steerers at the drift solenoids of the cooler were used to tilt the electron beam relative to the proton beam, whereby the cooling force was reduced.

The beam emittance was determined using the ionization profile monitor (IPM) (Sec. IV E), located in one of the COSY arcs. The detected beam profiles, shown in Fig. 10, were fitted by a Gaussian, providing the beamwidths. In Fig. 21 the expansion of the beam size is illustrated. The beam was completely cooled to widths of about $2\sigma_x = 3.2 \text{ mm}$ (continuous red line) and $2\sigma_y = 2.0 \text{ mm}$ (dashed blue line) and then expanded to a larger equilibrium beam size by tilting the electron beam.

Using the appropriate β -functions from the MAD model at the location of the IPM ($\beta_x = 12.6 \text{ m}$ and $\beta_y = 9.6 \text{ m}$), allows one to determine the 2σ beam emittance ϵ_x and ϵ_y using (15). The obtained beam lifetimes are plotted in Fig. 22 (blue symbols) vs the four-dimensional beam emittance [85] (see footnote¹)

$$\epsilon = \epsilon_x \cdot \epsilon_y, \tag{34}$$

where it should be noted that the actual definition of the combined beam emittance is of minor importance.

The beam lifetime increased with increasing beam emittance and an improvement from $\tau_b = 6300$ s to 9200 s was achieved. For emittances $\epsilon > 3 \ \mu m^2$, corresponding to



FIG. 22. Measured beam lifetime τ_b and calculated maximal incoherent tune shift $-\Delta Q_{x,y}^{\text{inc}}$ from (35) as a function of the fourdimensional beam emittance [see (34)]. The beam lifetime (blue dots) increases from 6300 to 9200 s with increasing beam emittance. The lines are shown to guide the eye.

electron beam tilt angles of ≥ 0.3 mrad, the cooling performance was very poor and therefore, two data points were omitted from the analysis.

In the following, we discuss the observed increase of the beam lifetime with increasing beam emittance in terms of tune shifts. The Coulomb force between charged particles in a beam causes repulsion, which leads to defocusing in both transverse planes and therefore to a reduction of the tune Q.

For a nonuniform charge distribution, the defocusing space-charge force is not linear with respect to the transverse coordinates. Therefore, each individual particle experiences a different tune shift. This betatron amplitude-dependent detuning, called tune spread, represents a certain area in the tune diagram. Assuming a Gaussian beam distribution, the incoherent tune shifts of the central particles in the beam, i.e., the maximal tune shifts, in the horizontal and vertical phase space are described by [86]

$$\Delta Q_{x,y}^{\rm inc} = -\frac{r_0 N}{\pi \beta_L^2 \gamma_L^3} \cdot \frac{F_{x,y} G_{x,y}}{B_f} \frac{1}{\epsilon_{x,y} + \sqrt{\epsilon_x \cdot \epsilon_y}}.$$
 (35)

Here r_0 is the classical proton radius, N is the number of particles in the accelerator, β_L and γ_L are the Lorentz factors, $\epsilon_{x,y}$ denote the horizontal and vertical emittances, respectively, and B_f is the bunching factor. For an unbunched beam as used in the experiment $B_f = 1$. $G_{x,y}$ is a form factor depending on the particle distribution inside the beam. Here G = 2 representing a Gaussian distribution was used. The form factor $F_{x,y}$, which can be derived from Laslett's image coefficients for incoherent tune shifts [87], was set to unity because the beam energy is small.

The tune measurement technique at COSY, based on the excitation of coherent transverse oscillations of the beam (see Sec. VA), however, is insensitive to incoherent tune shifts. The calculated incoherent tune shift $|\Delta Q_{x,y}^{inc}|$ decreases with increasing beam emittance [see (35)], the associated area in the tune diagram shrinks, fewer betatron resonances are excited, and therefore the measured beam lifetime increases. This theoretical consideration is consistent with the results shown in Fig. 22. For the smallest achieved beam emittances of about $\epsilon = 0.2\mu m^2$, the maximum tune shift amounts to $|\Delta Q_{x,y}^{inc}| \approx 0.1$, thus with a nominal tune of $Q_{x,y} = 3.6$ strong second-order betatron resonances at $Q_{x,y} = 3.5$ are intersected.

B. Contributions from vacuum to beam lifetime

In this section, the different contributions to the beam lifetime from the machine vacuum and the PAX target are discussed. In order to minimize the beam losses due to the gas load from the ABS in the PAX target chamber and the adjacent up- and downstream sections, a dedicated vacuum system (see Sec. III C) was implemented.

The contributions to the total beam lifetime can be written as

$$\frac{1}{\tau_b} = \frac{1}{\tau_{\text{cell}}} + \frac{1}{\tau_{\text{low}\beta}} + \frac{1}{\tau_{\text{ring}}},$$
(36)

where τ_{cell} denotes the single-scattering losses in the storage cell, $\tau_{low\beta}$ those from the gas load elsewhere inside the low- β section, and τ_{ring} is the contribution from the ring, independent of whether the PAX target was on or off.

After setting up the proton beam at $T_p = 49.3$ MeV (described in Sec. IX), a maximal beam lifetime of $\tau_{\rm ring} \approx 12000$ s was achieved without gas feed to the storage cell of the target setup. When the gas feed was switched on, typical total beam lifetimes of about $\tau_b \approx 8000$ s were routinely provided during the spin-filtering experiments (see Fig. 23).

The beam lifetime from single-scattering losses at the target, caused by those mechanisms that cannot be compensated by electron cooling, i.e., hadronic (σ_0) and single Coulomb scattering (σ_c), is given by

$$\tau_{\text{cell}} = ([\sigma_C + \sigma_0] \cdot d_t f)^{-1}, \qquad (37)$$

where $f \approx 508$ kHz denotes the revolution frequency. The total hadronic cross section $\sigma_0 = 59.8$ mb was extracted from the SAID database [88], and the Coulomb loss cross section [see (8)] was determined from the machine acceptance angle at the target, $\Theta_{\rm acc} = 6.45 \pm$ 0.27 mrad (see Table V), yielding $\sigma_C = 677.6$ mb. The resulting beam lifetime from (37) yields $\tau_{\rm cell} = 48500$ s with $d_t = 5.5 \times 10^{13}$ cm⁻² [see (14)].

The contribution from single-scattering loss outside the cell in the low- β section, determined from (36), yields $\tau_{\text{low}\beta} = (\tau_b^{-1} - \tau_{\text{ring}}^{-1} - \tau_{\text{cell}}^{-1})^{-1} = 47500 \text{ s.}$ The three contributions to the total beam lifetime are summarized



FIG. 23. Beam current as a function of time for a typical spin filtering run, indicating a beam lifetime of $\tau_b = 8000$ s with the polarized hydrogen target switched on. At the end of the cycle, the much denser unpolarized deuterium cluster target is switched on to determine the resulting beam polarization. The total duration of the shown cycle amounts to ≈ 5.5 h.

in Table VI. The results show that the total beam lifetime at COSY is dominated by the machine alone, whereas the target region contributes only one third.

IX. SPIN FILTERING AT 49.3 MEV

The goal of machine development was to provide a routine to set up COSY for the spin-filtering experiments. This routine (see Sec. IX A) and the measurement cycles (see Sec. IX B) are described below. Major requirements for the experiment were beam intensities of about 1×10^{10} protons and long beam and polarization lifetimes. Dedicated cycles were set up to measure the beam polarization lifetime (see Sec. IX C), and the efficiency of the rf spin flipper (see Sec. IX D) enabling the application of the cross-ratio method [89] within each cycle by reversing the beam polarization.

A. Setting up the beam

Based on the investigations described above, the following sequence of steps was applied to provide long beam and polarization lifetimes together with high beam intensities: (i) setting up injection for protons at $T_p = 45$ MeV with standard COSY optics; (ii) setting up electron cooling,

TABLE VI. Contributions to the total beam lifetime of $\tau_b = 8000$ s during the spin-filtering experiments with polarized target with $d_t = 5.5 \times 10^{13}$ cm⁻².

Losses due to		
Single scattering in the storage cell	$ au_{\mathrm{cell}}$	48500 s
Gas load elsewhere in the low- β section	$\tau_{\mathrm{low}\beta}$	47500 s
Machine vacuum alone	$ au_{ m ring}$	12000 s

including the transverse feedback system; (iii) first closed orbit correction; (iv) switching on the low- β section by increasing the current in the low- β quadrupoles and simultaneously decreasing the current in the quadrupoles of the target telescope, while keeping the machine tunes constant (see Sec. VI); (v) optimization of injection and electron cooling with the low- β section switched on; (vi) setting up stacking injection to increase the beam intensity; (vii) second closed orbit correction; (viii) setting up acceleration to $T_p = 49.3$ MeV with electron beam switched off; (ix) setting up electron cooling without feedback with reduced electron current ($I_{e} = 50$ mA) for optimal beam lifetime; (x) change of machine optics to dispersion D = 0 setting; (xi) third closed orbit correction; (xii) tune adjustment (using only QU1, QU5 and QU2, QU6, Fig. 1, to keep D = 0) to provide optimal beam lifetime without transverse feedback; (xiii) adjustment of electron beam angle with respect to the proton beam to further optimize the beam lifetime (see Sec. VIII A).

Concerning step (ix) it should be noted that it proved more effective to operate the transverse feedback system of the electron cooler (see Sec. II A) at injection energy rather than at the experiment energy of 49.3 MeV. The excitation of coherent betatron oscillations in the beam, due to the lack of transverse feedback at experiment energy, was avoided by selecting a different working point $(Q_x = 3.62 \text{ and } Q_y = 3.64)$ and by a reduction of the electron current.

B. Measurement cycle

After the beam had been set up as described in Sec. IX A, a dedicated spin-filtering cycle was implemented according to the sequence shown in Fig. 24. The relevant figure of merit can be expressed as FOM = $P^2(t) \cdot I(t)$ [90] which led to the decision to use filtering periods of 1.5 and 2 beam lifetimes to yield the smallest overall uncertainties for the spin-dependent cross sections [16], while at the same time providing the time dependence of the polarization buildup. A cycle with no filtering but otherwise identical settings as in the spin filtering process was set up for systematic studies.



FIG. 24. Sequence of two spin-filtering cycles. During the polarization buildup the polarized internal target and the holding field were switched on, with the ABS chopper open, and the magnetic holding field along the *y* axis. The BRP was used to measure the target polarization. After spin filtering the ABS chopper was closed and the ANKE cluster target together with the ANKE DAQ were switched on to measure the proton-beam polarization. The electron-cooler current was increased to compensate for larger energy losses due to the thicker cluster target. During the measurement period the beam polarization was flipped several times to minimize systematic effects. The holding field polarity was reversed after each spin-filtering cycle.

The spin-filtering cycles were composed of three parts. Beam preparation (56 s): An unpolarized proton beam was injected at a beam energy of $T_p = 45$ MeV, electron cooled ($I_e = 150$ mA) and subsequently accelerated to $T_p = 49.3$ MeV.

Spin filtering ($t_{\text{filter}} = 0$, 12000, and 16000 s): Polarized hydrogen atoms were injected into the storage cell at the PAX interaction point. The holding field coils, orienting the target polarization, were powered on in either +y (up) or -y (down) orientation for the duration of the spin-filtering period. Three different spin-filtering periods were used: $t_{\text{filter}} = 12000$ s and $t_{\text{filter}} = 16000$ s, corresponding to about 1.5 and 2 times the measured beam lifetime. For systematic reasons measurements with $t_{\text{filter}} = 0$ s were taken as well.

Beam polarimetry (2500 s): At the end of the spinfiltering period, the PAX polarized target was switched off, the ANKE deuterium cluster target was switched on, and the data acquisition for the determination of the beam polarization was started (Sec. IV G). The current of the electron cooler was increased from $I_e = 50$ to 100 mA. Reversing the beam polarization during this period, utilizing the spin flipper [91], allowed one to determine the induced beam polarization within each cycle, thereby reducing systematic errors.

C. Measurement of the polarization lifetime

In order to avoid depolarization of the beam during spin filtering, the betatron tunes were set far away from depolarizing resonances [40]. These arise when the horizontal and vertical tunes, the orbit frequency, and the synchrotron frequency, or combinations thereof, are synchronous with the spin tune. The spin tune ν_s , the number of precessions of the spin vector around the vertical axis per beam revolution in the ring, is defined as

$$\nu_{\rm s} = \gamma_L G, \tag{38}$$

where G = 1.792847 [77] is the proton anomalous magnetic moment, and γ_L the Lorentz factor. In a strong focusing synchrotron such as COSY, two different types of first-order spin resonances are excited. *Imperfection resonances* are caused by magnetic field errors and misalignments of the magnets, for which the condition is given by $\gamma_L G = k$, with $k \in \mathbb{N}$. *Intrinsic resonances* are excited by horizontal fields due to vertical focusing. For these the condition is given by $\gamma_L G = kP \pm Q_y$, where P is the superperiodicity of the lattice, and Q_y the vertical tune. *Higher-order resonances* can depolarize a stored beam as well, when the condition $\nu_s = k \pm lQ_x \pm mQ_y$, with $k, l, m \in \mathbb{Z}$ is fulfilled.

The polarization lifetime τ_P was measured in order to assess its effect on the final beam polarization after spin filtering. Figure 25 shows the cycle setup schematically. The beam was injected into COSY and accelerated to



FIG. 25. Measurement cycle to determine the beam polarization lifetime. The beam polarization (red) is measured before (P_i) and after (P_f) a waiting period of 5000 s. During the measurement, the deuterium cluster target (CT) of the ANKE polarimeter is switched on causing a faster decrease of the beam intensity (black).

 $T_p = 49.3$ MeV in exactly the same way as for the spinfiltering cycle, the only difference being that a polarized beam with $P \approx 0.75$ was injected, provided by the polarized ion source of COSY (see Sec. II). The initial beam polarization P_i was determined during a time period of $t_1 = 300$ s using the beam polarimeter at the ANKE target place (see Sec. IV G). Subsequently, the cluster target was switched off for $t_2 = 5000$ s in order to minimize beam losses. The measurement of the final polarization P_f lasted for $t_3 = 940$ s. The durations of the measurement periods were optimized to yield the smallest relative errors in τ_P and to achieve equal statistical errors of the beam polarization during both sequences. The beam polarization lifetime was determined by evaluating

$$\tau_P = \frac{-\Delta t}{\ln(\frac{P_f}{P_i})},\tag{39}$$

which exploits the exponential decay of the beam polarization as a function of time [92]. The initial and the final beam polarizations were averaged over the measurement periods t_1 and t_3 , respectively. Taking these measurement periods into account, the time difference between the two polarization measurements is given by $\Delta t = t_2 + t'_1 + t'_3 =$ 5496 s, where t'_1 and t'_3 account for the exponential decrease of the event rate within each measurement period. With $P_i = 0.746 \pm 0.003$ and $P_f = 0.731 \pm 0.003$ [93], the determination of the polarization lifetime yielded

$$\tau_P = (2.7 \pm 0.8) \times 10^5 \text{ s.}$$
 (40)

Therefore, the polarization losses during the spin-filtering experiments with filter times of $t_{\text{filter}} = 12000$ and 16000 s did not exceed 6%.

D. Efficiency of rf spin flipper

During the polarization measurement period at the end of each filtering cycle, the beam polarization was flipped several times to enable the beam polarization to be determined within each cycle using the cross-ratio method [89], whereby systematic errors are canceled to first order.

The spin flips were generated using a Froissart-Stora frequency sweep induced with an rf solenoid [91,94]. The rf frequency was swept over the precession frequency of the proton spin and flipped the spin resonantly at the frequency $f_{\rm rf} = f_0 \cdot (\gamma_L G \pm k)$, which yielded $f_{\rm rf} = 0.9620$ MHz for k = 0. The frequency ramp from 0.9605 to 0.9625 MHz was carried out in 2.5 s, therefore the effect on the duty cycle was negligible.

The spin flip efficiency,

$$\varepsilon_{\rm flip} = \exp\left(\frac{\ln\left(\frac{|P_f|}{|P_i|}\right)}{n_{\rm flip}}\right),\tag{41}$$

where $P_{i,f}$ are the initial and final polarizations, was determined in order to be able to correct for polarization losses and to adjust the number of flips n_{flip} within the measurement period. Since the change of sign of the polarization after each flip is not relevant for the presented analysis, the absolute values of $P_{i,f}$ are used to determine the flip efficiency.

A dedicated cycle was used to measure the efficiency of the spin flipper during commissioning and regularly during the experiment. This cycle, shown schematically in Fig. 26, yielded the smallest relative error in $\varepsilon_{\text{flip}}$. It begins with the injection and acceleration of a polarized proton beam $(P \approx 0.75)$ to $T_p = 49.3$ MeV, followed by a polarization measurement lasting for about 50 s. Subsequently, the cluster target was switched off and $n_{\text{flip}} = 99$ spin flips



FIG. 26. Measurement cycle to determine the spin-flip (SF) efficiency. The beam polarization (red) is measured before (P_i) and after (P_f) $n_{\text{flip}} = 99$ spin flips. While these spin-flips are being executed, the deuterium cluster target (CT) of the ANKE polarimeter is switched off.

were performed within a time period of 300 s. An odd number of spin flips was chosen to guarantee the presence of spin flips by observing a sign reversal of the final polarization. Finally, the beam polarization was measured again for about 100 s.

The three measurements of $\varepsilon_{\rm flip}$ during the experiment period, each lasting for about two hours, yielded in average

$$\varepsilon_{\rm flip} = 0.9872 \pm 0.0001.$$
 (42)

During the initial spin-filtering measurements there were two spin flips. Thus, the polarization loss due to the spinnever exceeded 3%.

X. CONCLUSION

In this paper, we present the machine development for the spin-filtering experiments carried out at COSY [28]. The prime objective was to provide a long beam lifetime in the presence of a polarized hydrogen gas target. To this end, a dedicated low- β section consisting of two quadrupole doublets was implemented at the PAX target place. The optimization of the beam lifetime included the search for optimal working points, closed orbit corrections, optimization of electron cooling, and the minimization of the β -functions at the PAX target.

The low- β insertion led to β -functions of $(\beta_x, \beta_y) = (0.31 \pm 0.03 \text{ m}, 0.46 \pm 0.05 \text{ m})$ at the center of the polarized storage cell target, resulting in a reduction of about a factor of 10 compared to the situation before. Hence, single Coulomb scattering as the dominating loss mechanism for cooled beams was reduced by the same factor. In addition, this allowed us to use a narrow storage cell of diameter d = 9.6 mm and length l = 400 mm with an areal targetgas density of $d_i = (5.5 \pm 0.2) \times 10^{13}$ atoms/cm².

Special attention was given to the vacuum conditions in and around the target chamber through the installation of a sophisticated pumping system together with flow limiters at the entrance and exit of the chamber. The beam lifetime caused by the target region with an injected gas flow of 3.3×10^{16} H/s contributed only one third to the total beam lifetime of $\tau_b = 8000$ s, while the contribution of the machine itself was twice as large.

The machine acceptances, the beamwidths, and the machine acceptance angle at the target were determined using a dedicated movable frame system, yielding $A_x = (31.2 \pm 2.5) \,\mu\text{m}$, $A_y = (15.7 \pm 1.8) \,\mu\text{m}$, $(2\sigma_x, 2\sigma_y) = (1.03 \pm 0.01 \text{ mm}, 0.67 \pm 0.02 \text{ mm})$, and $\Theta_{\text{acc}} = (6.45 \pm 0.27) \text{ mrad}$. With the achieved β -functions, the horizontal and vertical 2σ beam emittances were $\epsilon_x = (1.71 \pm 0.17) \,\mu\text{m}$ and $\epsilon_y = (0.92 \pm 0.15) \,\mu\text{m}$, respectively.

In order to improve the systematics of the spin-filtering experiment, an rf spin flipper was utilized to reverse the polarization of the stored beam after spin filtering. The spin-flip efficiency determined in dedicated cycles amounted to $\varepsilon_{\rm flip} = 0.9872 \pm 0.0001$, and the polarization loss due to the spin flipper never exceeded 3%. In addition, the polarization lifetime was determined in dedicated cycles, yielding $\tau_P = (2.7 \pm 0.8) \times 10^5$ s. Thus for the spin-filtering experiments at COSY with spin-filtering times of $t_{\rm filter} = 12000$ and 16000 s, the polarization loss due to a finite polarization lifetime did not exceed 6%.

The interplay of the investigations presented in this paper fulfilled the demanding beam conditions for the first spin-filtering experiment at COSY. The presented results comprise a recipe for setting up a beam for spin-filtering experiments in a storage ring, directly applicable to the anticipated spin-filtering studies with antiprotons at the AD of CERN [27].

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- [1] P.L. Csonka, Nucl. Instrum. Methods 63, 247 (1968).
- [2] K. Kilian and D. Möhl, Ettore Majorana international science series Physical science 17, 701 (1984).
- [3] Proceedings of the Workshop on Polarized Antiprotons, Bodega Bay, 1985, edited by A. D. Krisch, A. M. T. Lin, and O. Chamberlain, AIP Conf. Proc. No. 145 (AIP, New York, 1986); http://scitation.aip.org/content/ aip/proceeding/aipcp/145.
- [4] Proceedings of the International Workshop "Polarized antiproton beams-how?" Daresbury, UK, 2007, edited by D. P. Barber, N. Buttimore, S. Chattopadhyay, G. Court, and E. Steffens, AIP Conf. Proc. No. 1008 (AIP, New York, 2008); http://scitation.aip.org/content/aip/proceeding/ aipcp/1008.
- [5] The program of the 409th WE-Heraeus Seminar, including all talks, is available from http://www.fe.infn.it/heraeus/.
- [6] F. Rathmann *et al.*, Phys. Rev. Lett. **71**, 1379 (1993).

- [7] F. Rathmann, Ph.D. thesis, Philips-Universität Marburg, 1994.
- [8] K. Zapfe *et al.*, Nucl. Instrum. Methods Phys. Res., Sect. A 368, 293 (1996).
- [9] K. Zapfe et al., Rev. Sci. Instrum. 66, 28 (1995).
- [10] D. Oellers et al., Phys. Lett. B 674, 269 (2009).
- [11] A. Lehrach, O. Boine-Frankenheim, F. Hinterberger, R. Maier, and D. Prasuhn, Nucl. Instrum. Methods Phys. Res., Sect. A 561, 289 (2006).
- [12] FAIR Baseline Technical Report, edited by H. H. Gutbrod et al., ISBN 3-9811298-0-6 (2006), available from http:// www.fair-center.de/fileadmin/fair/publications_FAIR/ FAIR_BTR_1.pdf.
- [13] P. Lenisa and F. Rathmann (PAX Collaboration), Antiproton-proton scattering experiments with polarization (Letter of Intent), 2003, available from http://collaborations .fz-juelich.de/ikp/pax/documents/proposals.shtml.
- [14] V. Barone *et al.* (PAX Collaboration), Antiproton-proton Scattering experiments with polarization (Technical proposal), 2005, available from http://arxiv.org/pdf/hep-ex/ 0505054.pdf.
- [15] F. Bradamante, I. Koop, A. Otboev, V. Parkhomchuk, V. Reva, P. Shatunov, and Yu. Shatunov*et al.*, arXiv:physics/ 0511252.
- [16] F. Rathmann et al., Phys. Rev. Lett. 94, 014801 (2005).
- [17] A. I. Milstein and V. M. Strakhovenko, Phys. Rev. E 72, 066503 (2005).
- [18] N. N. Nikolaev and F. F. Pavlov, in *Proceedings of the* 17th International Spin Physics Symposium (SPIN 2006), Kyoto, 2006 (AIP, New York, 2007), Vol. 915, p. 932.
- [19] N. N. Nikolaev and F. F. Pavlov, AIP Conf. Proc. 1008, 34 (2008).
- [20] A. I. Milstein, S. G. Salnikov, and V. M. Strakhovenko, Nucl. Instrum. Methods Phys. Res., Sect. B 266, 3453 (2008).
- [21] R. Maier, Nucl. Instrum. Methods Phys. Res., Sect. A 390, 1 (1997).
- [22] D. Oellers *et al.*, Nucl. Instrum. Methods Phys. Res., Sect. A **759**, 6 (2014).
- [23] V. F. Dmitriev, A. I. Milstein, and S. G. Salnikov, Phys. Lett. B 690, 427 (2010).
- [24] D. Zhou and R. G. E. Timmermans, Phys. Rev. C 87, 054005 (2013).
- [25] Y. N. Uzikov and J. Haidenbauer, Phys. Rev. C 87, 054003 (2013).
- [26] Y. N. Uzikov, J. Haidenbauer, and B. A. Prmantayeva, Phys. Rev. C 84, 054011 (2011).
- [27] P. Lenisa and F. Rathmann (PAX Collaboration), Measurement of the spin dependence of the $\bar{p}p$ interaction at the AD ring, 2009, available from http://arxiv.org/abs/0904 .2325.
- [28] W. Augustyniak et al., Phys. Lett. B 718, 64 (2012).
- [29] N. S. P. King, J. L. Romero, J. Ullmann, H. E. Conzett, R. M. Larimer, and R. Roy, Phys. Lett. 69B, 151 (1977).
- [30] J. Bystricky, F. Lehar, and P. Winternitz, J. Phys. II (France) 39, 1 (1978).
- [31] C. Weidemann, Ph.D. thesis, University of Cologne, 2011, available from http://collaborations.fz-juelich.de/ikp/pax/ public_files/theses/thesisCh.Weidemann.pdf.

- [32] D. Prasuhn et al., in Proceedings of the Workshop on Beam Cooling and Related Topics, Montreux, 1993 [CERN Report No. 94-03, 317-321 1994].
- [33] D. Prasuhn, J. Dietrich, R. Maier, R. Stassen, H. J. Stein, and H. Stockhorst, Nucl. Instrum. Methods Phys. Res., Sect. A 441, 167 (2000).
- [34] P. D. Eversheim et al., in Proceedings of the International Symposium on High Energy Spin Physics SPIN 1996, Amsterdam, Netherlands (World Scientific, Singapore, 1997), p. 306.
- [35] L. Aldea, W. Bräutigam, R. Brings, C. Mayer-Böricke, J. Reich, and P. Wucherer, in *Proceedings of the 9th International Conference on Cyclotrons and their Applications, Caen, France, 1981*, edited by G. Gendreau (Les Editions de Physique, Paris, 1982), p. 103.
- [36] H. Stockhorst, Polarized proton and deuteron beams at COSY (2004), available from http://arxiv.org/abs/physics/ 0411148.
- [37] B. Lorentz, R. Gebel, A. Lehrach, R. Maier, D. Prasuhn, and H. Stockhorst, J. Phys. Conf. Ser. 295, 012146 (2011).
- [38] A. Lehrach et al., AIP Conf. Proc. 667, 30 (2003).
- [39] K. Bongardt, S. Martin, P. F. M. Meads, D. Prasuhn, H. Stockhorst, and R. Wagner, in *Proceedings of the IEEE Particle Accelerator Conference : Accelerator Science and Technology (PAC 89), Chicago, 1989.*
- [40] A. Lehrach, R. Gebel, R. Maier, D. Prasuhn, and H. Stockhorst, Nucl. Instrum. Methods Phys. Res., Sect. A 439, 26 (2000).
- [41] K. Wille, *The Physics of Particle Accelerators* (Oxford University Press, Oxford, 2001).
- [42] H. J. Stein, D. Prasuhn, H. Stockhorst, J. Dietrich, K. Fan, V. Kamerdzhiev, R. Maier, I. N. Meshkov, A. Sidorin, and V. V. Parkhomchuk, arXiv:1101.5963.
- [43] H. J. Soltner, H. Stein, V. Kamerdzhiev, J. de Villiers, J. Conradie, and J. Dietrich, IEEE Trans. Appl. Supercond. 24, 1 (2014).
- [44] V. Kamerdzhiev, Ph.D. thesis, Dortmund University, 2003, available from https://eldorado.tu-dortmund.de/bitstream/ 2003/2322/1/Kamerdzhievunt.pdf.
- [45] V. Kamerdzhiev, J. Dietrich, R. Maier, I. N. Meshkov, I. Mohos, D. Prasuhn, A. Sidorin, H. J. Stein, and H. Stockhorst, Nucl. Instrum. Methods Phys. Res., Sect. A 532, 285 (2004).
- [46] N. Madsen, S. Maury, and D. Möhl, Nucl. Instrum. Methods Phys. Res., Sect. A 441, 54 (2000).
- [47] H. Poth, Phys. Rep. 196, 135 (1990).
- [48] C. Ekström et al., Phys. Scr. T22, 256 (1988).
- [49] H. Grote and F. C. Iselin, The MAD program (methodical accelerator design) version 8.4: User's reference manual, 1991, available from http://mad.web.cern.ch/mad/.
- [50] F. Stock *et al.*, Nucl. Instrum. Methods Phys. Res., Sect. A 343, 334 (1994).
- [51] A. Nass *et al.*, Nucl. Instrum. Methods Phys. Res., Sect. A 505, 633 (2003).
- [52] A. Airapetian *et al.* (HERMES Collaboration), Nucl. Instrum. Methods Phys. Res., Sect. A 540, 68 (2005).
- [53] G. Ciullo, L. Barion, C. Barschel, K. Grigoriev, P. Lenisa, A. Nass, J. Sarkadi, M. Statera, E. Steffens, and G. Tagliente, J. Phys. Conf. Ser. 295, 012150 (2011).

- [54] C. Baumgarten *et al.* (HERMES Target Group), Nucl. Instrum. Methods Phys. Res., Sect. A **482**, 606 (2002).
- [55] C. Baumgarten *et al.*, Nucl. Instrum. Methods Phys. Res., Sect. A 508, 268 (2003).
- [56] J. Price and W. Haeberli, Nucl. Instrum. Methods Phys. Res., Sect. A **349**, 321 (1994).
- [57] A. Roth, Vacuum Technology, 3rd ed. (Elsevier Science Publisher, Amsterdam, 1990).
- [58] H. J. Stein *et al.*, Phys. Rev. ST Accel. Beams **11**, 052801 (2008).
- [59] E. Steffens and W. Haeberli, Rep. Prog. Phys. 66, 1887 (2003).
- [60] F. Rathmann *et al.*, Phys. Rev. C 58, 658 (1998).
- [61] Integrated Engineering Software (IES), Winnipeg, Manitoba, Canada, http://www.integratedsoft.com.
- [62] P. Chiggiato and P. C. Pinto, Thin Solid Films 515, 382 (2006).
- [63] K. Unser, IEEE Trans. Nucl. Sci. 28, 2344 (1981).
- [64] R. Maier et al., in Proceedings of the 2nd European Particle Accelerator Conference (PAC 90), Nice, 1990.
- [65] J. Dietrich and I. Mohos, AIP Conf. Proc. 451, 454 (1998).
- [66] K. Grigoryev *et al.*, Nucl. Instrum. Methods Phys. Res., Sect. A **599**, 130 (2009).
- [67] C. Böhme, T. Weis, J. Dietrich, V. Kamerdzhiev, and J. L. Conradie, in *Proceedings of the 9th European Workshop* on Beam Diagnostics and Instrumentation for Particle Accelerators (DIPAC09), Basel, Switzerland, 2009, edited by J. Chrin, M. Marx, V. R. W. Schaa, and V. Schlott (PSI, Basel, 2009), p. 185.
- [68] P. Forck, in *Proceedings of the 1st International Particle* Accelerator Conference (IPAC'10), Kyoto, 2010.
- [69] H. J. Stein, IKP Annual Report (2004), available from http://donald.cc.kfa-juelich.de/wochenplan/publications/ AR2004/documents/AR2004_Articles.pdf.
- [70] A. Khoukaz, T. Lister, C. Quentmeier, R. Santo, and C. Thomas, Eur. Phys. J. D 5, 275 (1999).
- [71] R. Schleichert, T. Krings, S. Merzliakov, A. Mussgiller, and D. Protic, IEEE Trans. Nucl. Sci. 50, 301 (2003).
- [72] R. Cappi, E. Métral, and D. Möhl, in *Proceedings of the 18th International Conference, HEACC 2001* (Tsukuba, Japan, 2001), Report No. CERN-PS-2001-010-AE.
- [73] S. Y. Lee, *Accelerator Physics*, 2nd ed. (World Scientific, Singapore, 2004).
- [74] A. Lehrach, F. Rathmann, and J. Pretz (JEDI Collaboration), Search for permanent electric dipole moments at COSY, 2012, COSY proposal No. 216, available from http:// collaborations.fz-juelich.de/ikp/jedi/public_files/proposals/ EDM-COSY-Proposal_cover_02.05.2012.pdf.
- [75] R. Talman, in Frontiers of Particle Beams; Observation, Diagnosis and Correction, Lect. Notes Phys. Vol. 343, edited by M. Month and S. Turner (Springer, Berlin, 1989), pp. 4–45.
- [76] D. Welsch, Ph.D. thesis, Rheinische Friedrich-Wilhelms-Universität Bonn, 2009, available at http://hss.ulb.uni-bonn .de/2010/2082/2082.pdf.
- [77] A. Chao and M. Tigner, Handbook of Accelerator Physics and Engineering (3rd printing) (World Scientific, Singapore, 2006).
- [78] P. Bryant, A simple theory for weak betatron coupling, in CERN Accelerator School, Geneva, 207 (1994); http:// dx.doi.org/10.5170/CERN-1994-001.

- [79] E. Courant and H. Snyder, Ann. Phys. (N.Y.) 3, 1 (1958).
- [80] M. Ross *et al.*, Nucl. Instrum. Methods Phys. Res., Sect. A 326, 424 (1993).
- [81] K. Potter, Beam profiles, CERN Accelerator School, Gif-sur-Yvette, Paris, 1984, Yellow Report No. CERN 85-19, 301-317 (1984); http://dx.doi.org/10.5170/ CERN-1985-019-V-1.
- [82] F. Hinterberger and D. Prasuhn, Nucl. Instrum. Methods Phys. Res., Sect. A 279, 413 (1989).
- [83] A. Jansson *et al.*, Tevatron beam study report, available from http://beamdocs.fnal.gov/AD/DocDB/0003/000393/ 002/Scraping%20Report.pdf (2003).
- [84] G. Guignard, The General Theory of all Sum and Difference Resonances in a Three-dimensional Magnetic Field in a Synchrotron (CERN, Geneva, 1976).
- [85] J. Buon, in Proceedings of the 1993 Particle Accelerator Conference (PAC 93), Washington D.C., 1993.
- [86] K. Schindl, Space Charge, CERN Accelerator School, Zeuthen, Germany, 305 (2003).
- [87] L. Laslett, in Proceedings of Summer Study on Storage Rings, Accelerators and Experimentation at Super

High-Energies, Brookhaven, USA, 1963, edited by J. W. Bittner (BNL, Upton, NY, 1963), p. 324; eConf **C630610**, 324 (1963).

- [88] SAID, Nucleon-nucleon scattering database, Center for Nuclear Studies, Department of Physics, George Washington University, USA.
- [89] R. C. Hanna, in Proceedings of the 2nd International Symposium on Polarization Phenomena, Karlsruhe, 1965 (Birkhaeuser, Basel, 1966), p. 280.
- [90] G. G. Ohlsen and P. W. Keaton, Nucl. Instrum. Methods 109, 41 (1973).
- [91] V. S. Morozov, A. D. Krisch, M. A. Leonova, R. S. Raymond, V. K. Wong, K. Yonehara, D. Eversheim, F. Hinterberger, H. Rohdjeß, and K. Ulbrich, Phys. Rev. ST Accel. Beams 7, 024002 (2004).
- [92] H.O. Meyer et al., Phys. Rev. E 56, 3578 (1997).
- [93] Z. Bagdasarian, Master's thesis, Ivane Javakhishvili Tbilisi State University, 2012, available from http:// collaborations.fz-juelich.de/ikp/pax/public_files/theses/ thesisZ.Bagdasarian.pdf.
- [94] M. Froissart and R. Stora, Nucl. Instrum. Methods 7, 297 (1960).